

*Thermodynamic Analysis of  
Manufacturing Processes*

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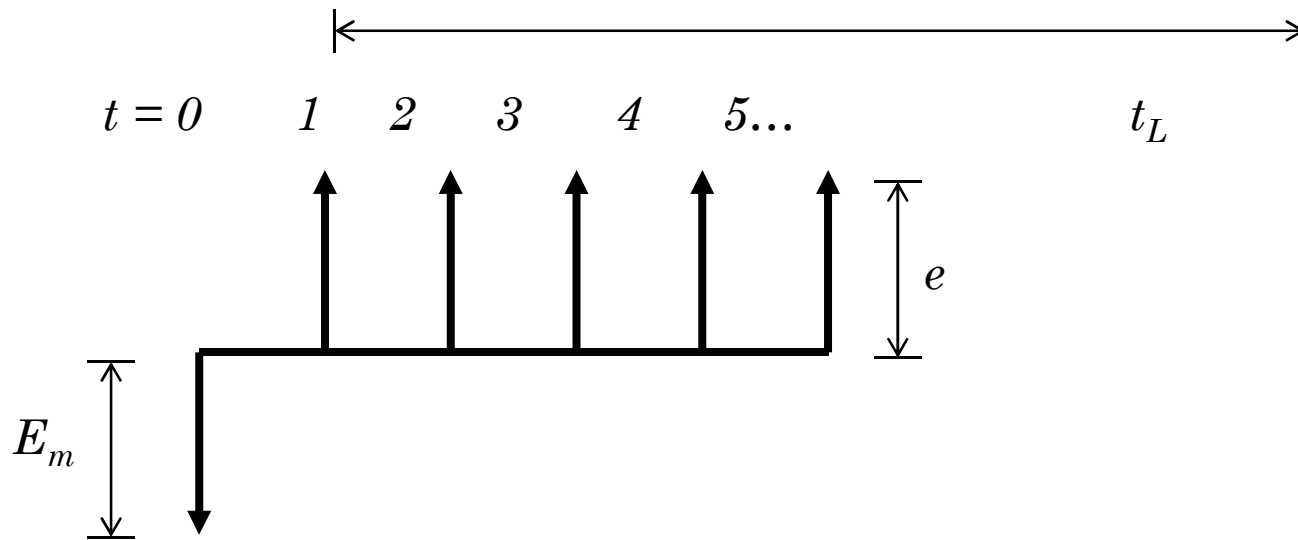
# Readings

1. *Exergy Ch 8, Cengel and Boles*
2. *Appendix, Szargut*
3. *Thermodynamic Analysis of Resources Used in Manufacturing Processes, Gutowski et al*

# *Role in “New Energy”*



# Energy Payback



*Time to breakeven =*

$$t_B = E_m/e$$

*Energy Return on Energy Investment =*

$$EROI = et_L/E_m$$

# *Efficiencies of Energy Production, “e”*

$$\eta_{II} = \frac{e_{out}}{e_{avail}}$$

$$e_{out} = \eta_{II} e_{avail}$$

*$\eta_{II}$*

PV: Shockley - Queisser Limit

Wind: Betz Limit

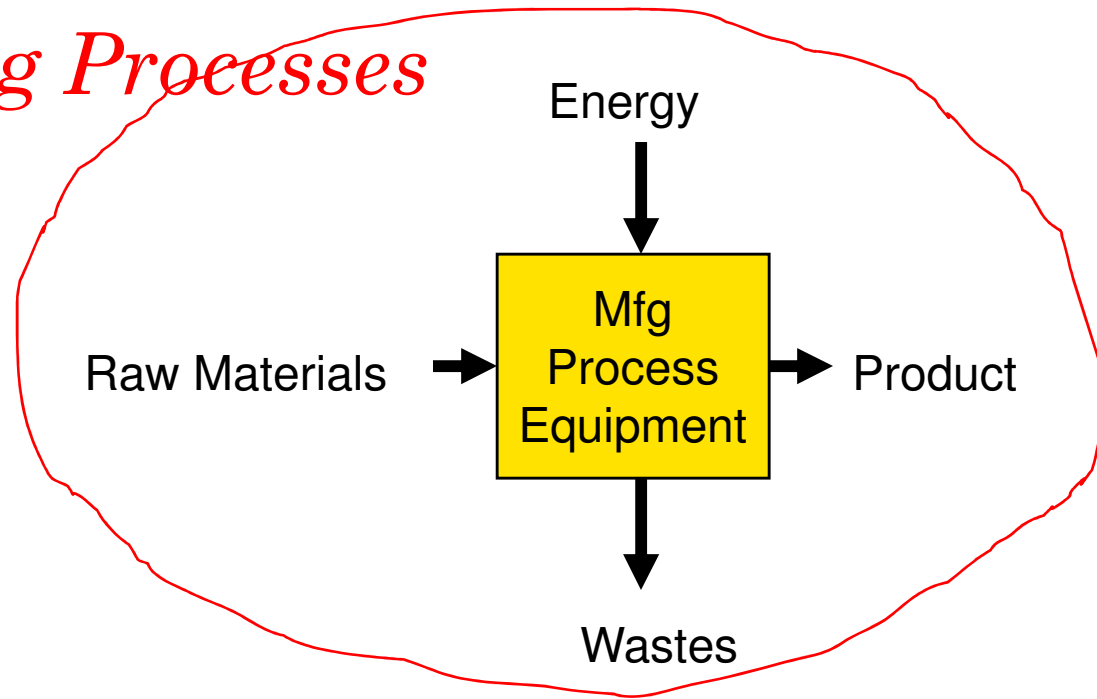
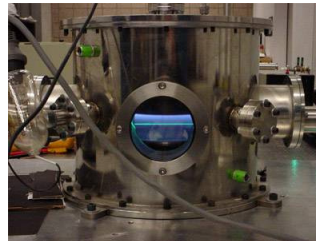
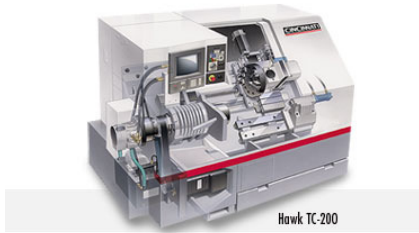
Nuclear: Carnot Limit

# *Efficiencies of Mfg Energy Requirement, “ $E_m$ ”*

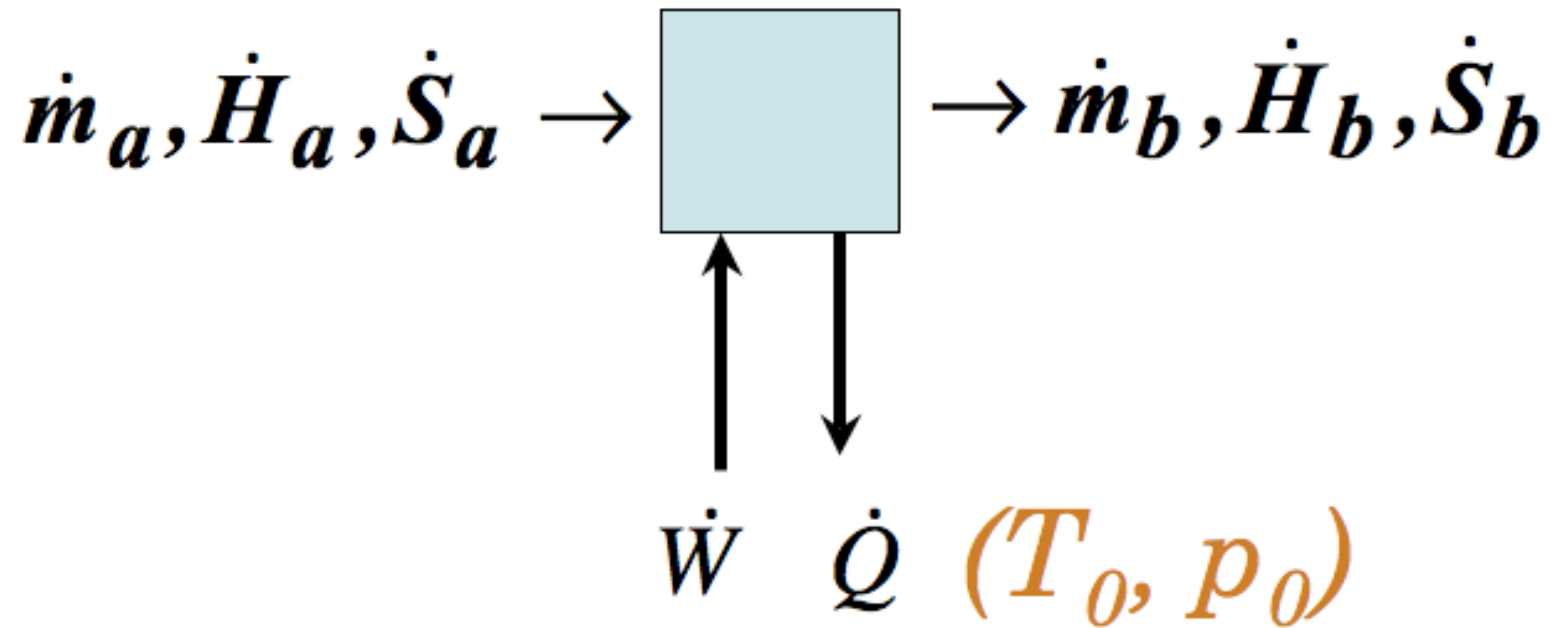
$$\eta = \frac{E_{\min}}{E_{\text{actual}}}$$

$$\eta = ?$$

# *Thermodynamic Analysis of Resources Used in Manufacturing Processes*



*Thermodynamic Analysis:  
Materials Transformation,  
Open System*





# *Balance Equations*

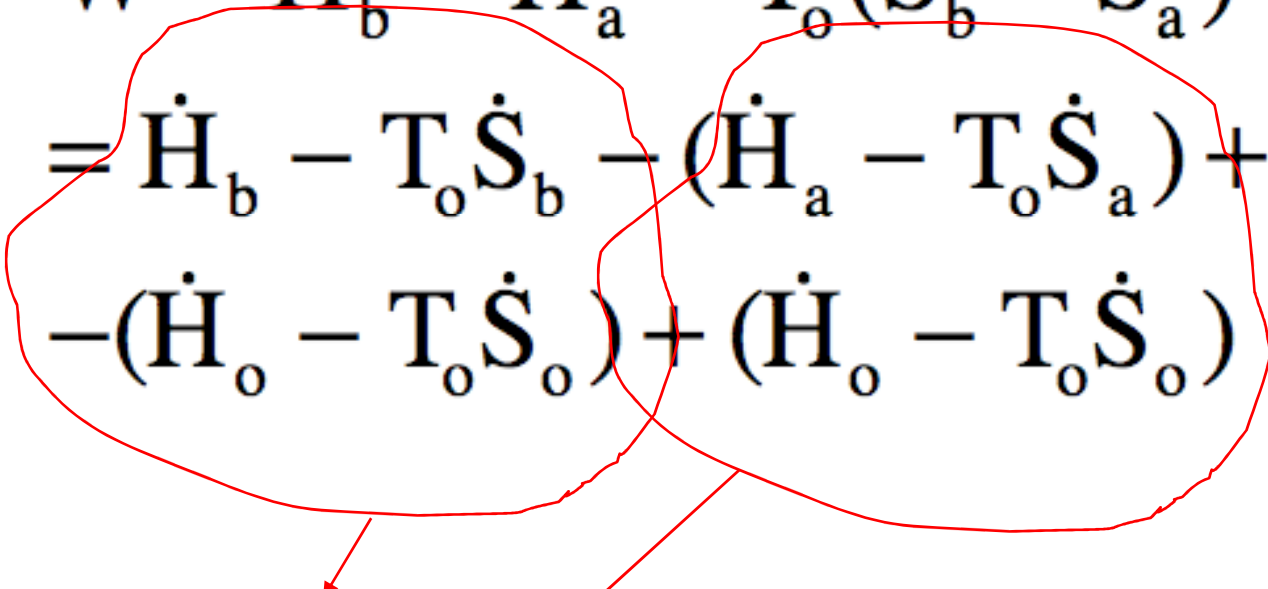
$$\frac{dM}{dt} = \dot{m}_a - \dot{m}_b = 0, \quad (\dot{m}_a = \dot{m}_b = \dot{m}) \quad \text{steady state}$$

$$\frac{dE}{dt} = \dot{H}_a + \dot{W} - \dot{Q} - \dot{H}_b = 0 \quad \text{steady state}$$

$$\frac{dS}{dt} = \dot{S}_a - \frac{\dot{Q}}{T_o} - \dot{S}_b + \dot{S}_{\text{irr}} = 0 \quad \text{steady state}$$

Eliminating  $\dot{Q}$ , gives Work Rate

$$\begin{aligned}\dot{W} &= \dot{H}_b - \dot{H}_a - T_o(\dot{S}_b - \dot{S}_a) + T_o\dot{S}_{irr} \\ &= \dot{H}_b - T_o\dot{S}_b - (\dot{H}_a - T_o\dot{S}_a) + T_o\dot{S}_{irr} \\ &\quad -(\dot{H}_o - T_o\dot{S}_o) + (\dot{H}_o - T_o\dot{S}_o)\end{aligned}$$


$$\dot{W} = \dot{B}_b - \dot{B}_a + T_o\dot{S}_{irr}$$

## *In terms of Minimum Work*

$$\dot{W} = \dot{B}_b - \dot{B}_a + T_o \dot{S}_{\text{irr}}$$

For the ideal case "reversible process"

$$(T_o \dot{S}_{\text{irr}} = 0) \quad w_{\text{min}} = \frac{\dot{W}}{\dot{m}} = b_b - b_a$$

intensive form, exergy per mole or mass, or

$$\text{extensive form } W_{\text{min}} = B_b - B_a$$

# *Exergy*

$$B = (H - T_o S) - (H_o - T_o S_o)$$

$$B = (H - H_o) - T_o (S - S_o)$$

$$dB = dH - T_o dS$$

$$B, X, Ex, E, \varepsilon$$

# *Open Systems, approximations for temperature and pressure dependence*

- Condensed phases

$$dh = c dT + v dp$$

$$ds = c dT/T$$

- Ideal gases

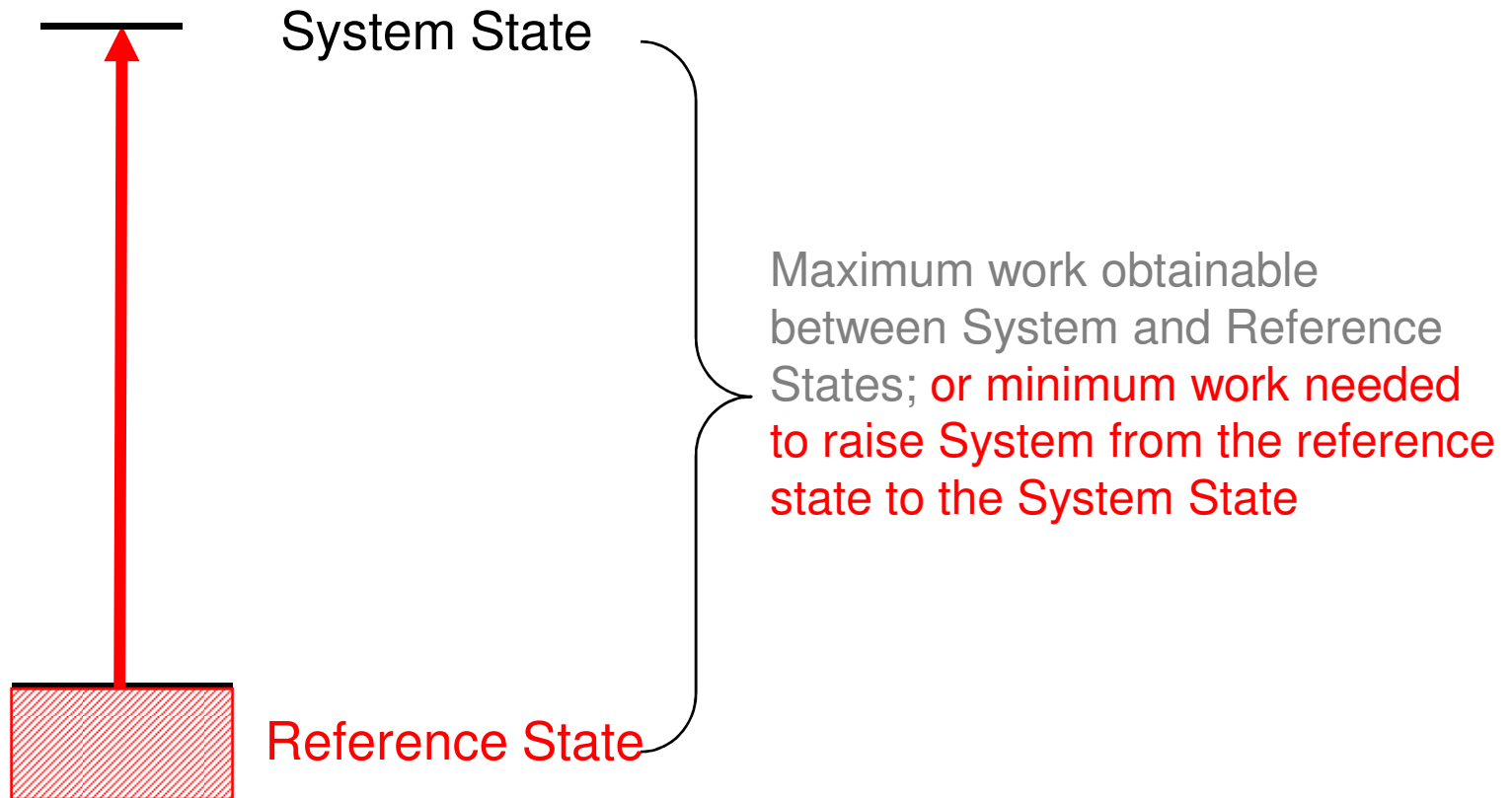
$$dh = c_p dT$$

$$ds = c_p dT/T - R dp/p$$

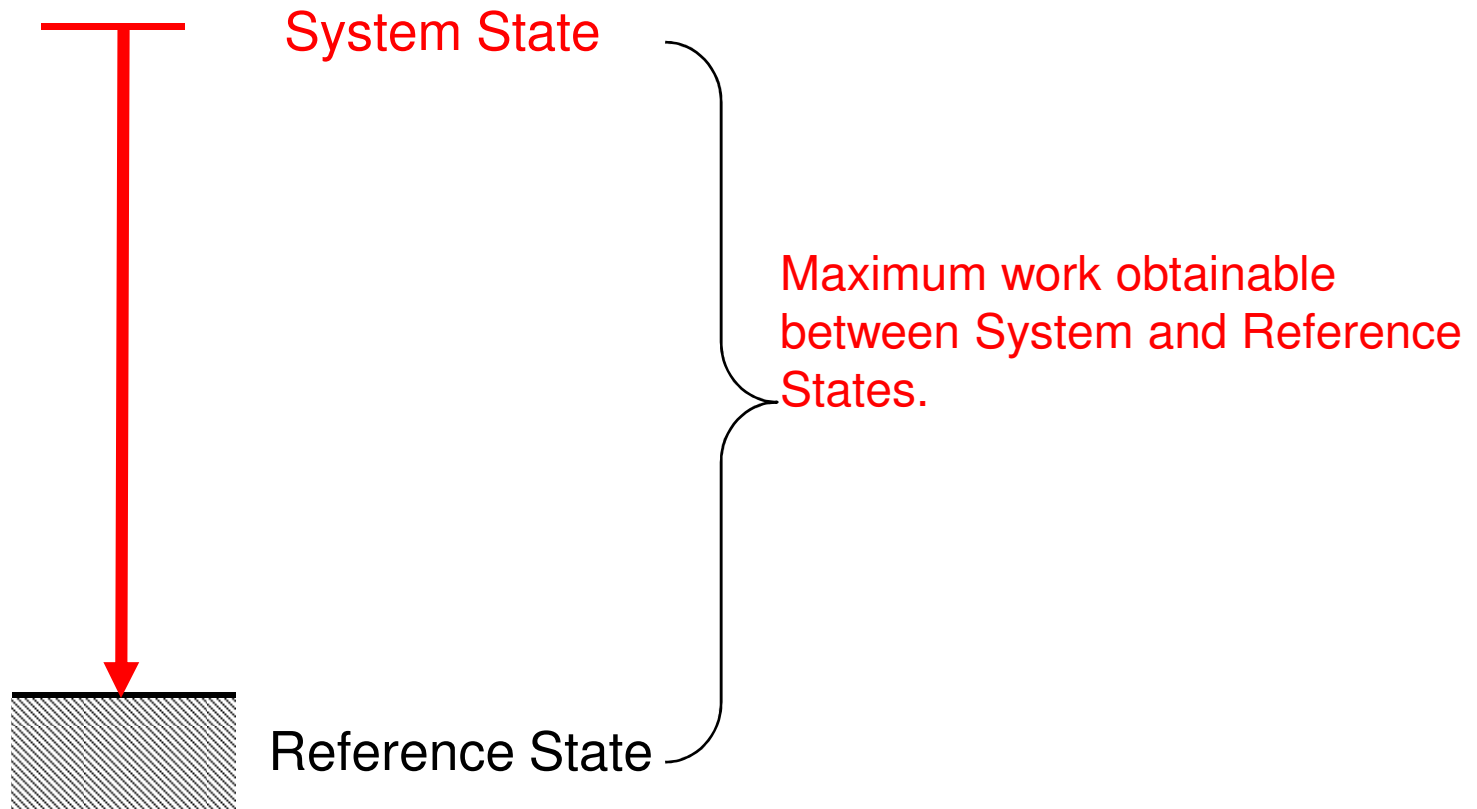
# Definition of Exergy “B”

“Exergy is the amount of work obtainable when some matter is brought to a state of thermodynamic equilibrium with the common components of the natural surroundings by means of reversible processes, involving interaction only with the above mentioned components of nature” [Szargut et al 1988].

# Exergy



# Exergy

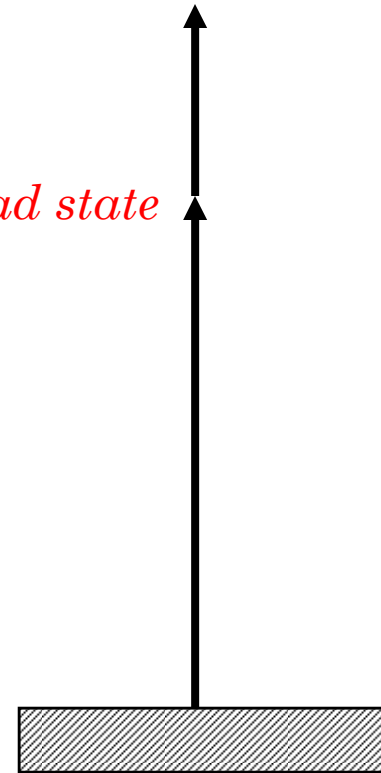




# *Types of Exergy*

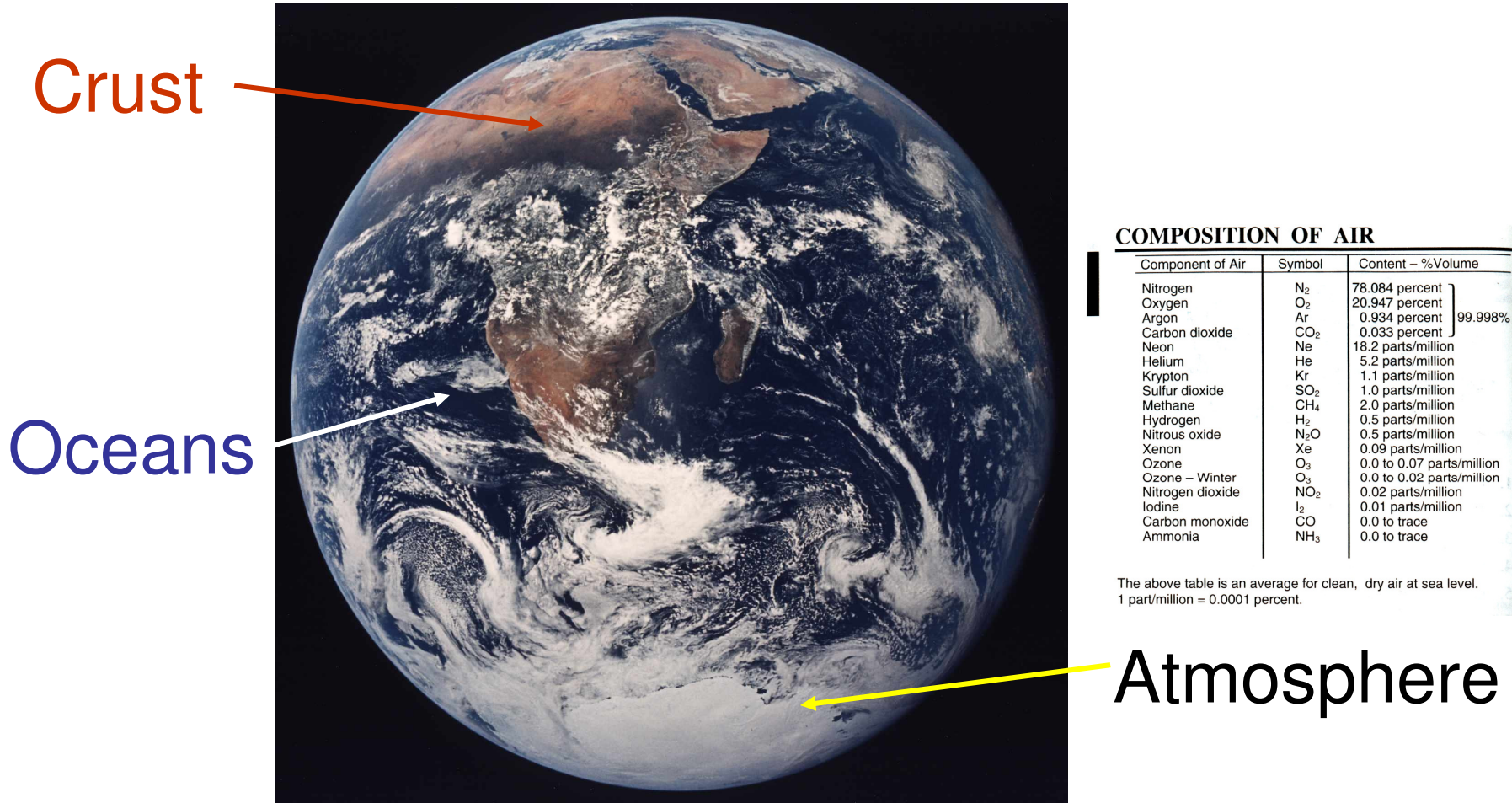
- Flow exergy (open systems)
  - Chemical
  - Mechanical
    - Temperature
    - Pressure
    - Kinetic energy
    - Potential energy
- Work interaction
- Heat interaction

*Restricted dead state  
 $T_0, P_0$*



*Dead state, e.g earth's crust  
at  $T_0, P_0$*

# Chemical Properties referenced to the “environment”



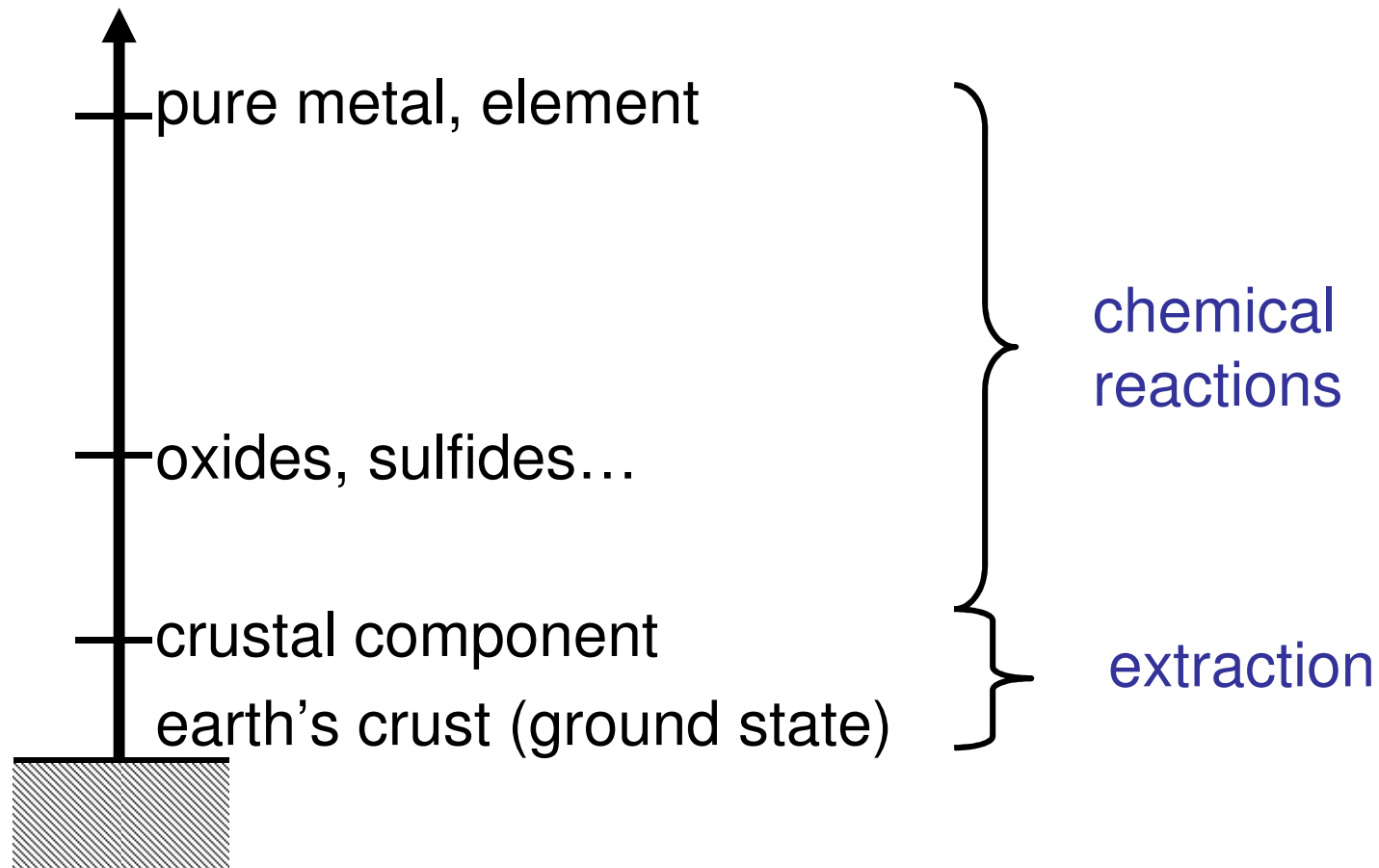
## COMPOSITION OF AIR

Component of Air	Symbol	Content – %Volume
Nitrogen	N <sub>2</sub>	78.084 percent
Oxygen	O <sub>2</sub>	20.947 percent
Argon	Ar	0.934 percent
Carbon dioxide	CO <sub>2</sub>	0.033 percent
Neon	Ne	18.2 parts/million
Helium	He	5.2 parts/million
Krypton	Kr	1.1 parts/million
Sulfur dioxide	SO <sub>2</sub>	1.0 parts/million
Methane	CH <sub>4</sub>	2.0 parts/million
Hydrogen	H <sub>2</sub>	0.5 parts/million
Nitrous oxide	N <sub>2</sub> O	0.5 parts/million
Xenon	Xe	0.09 parts/million
Ozone	O <sub>3</sub>	0.0 to 0.07 parts/million
Ozone – Winter	O <sub>3</sub>	0.0 to 0.02 parts/million
Nitrogen dioxide	NO <sub>2</sub>	0.02 parts/million
Iodine	I <sub>2</sub>	0.01 parts/million
Carbon monoxide	CO	0.0 to trace
Ammonia	NH <sub>3</sub>	0.0 to trace

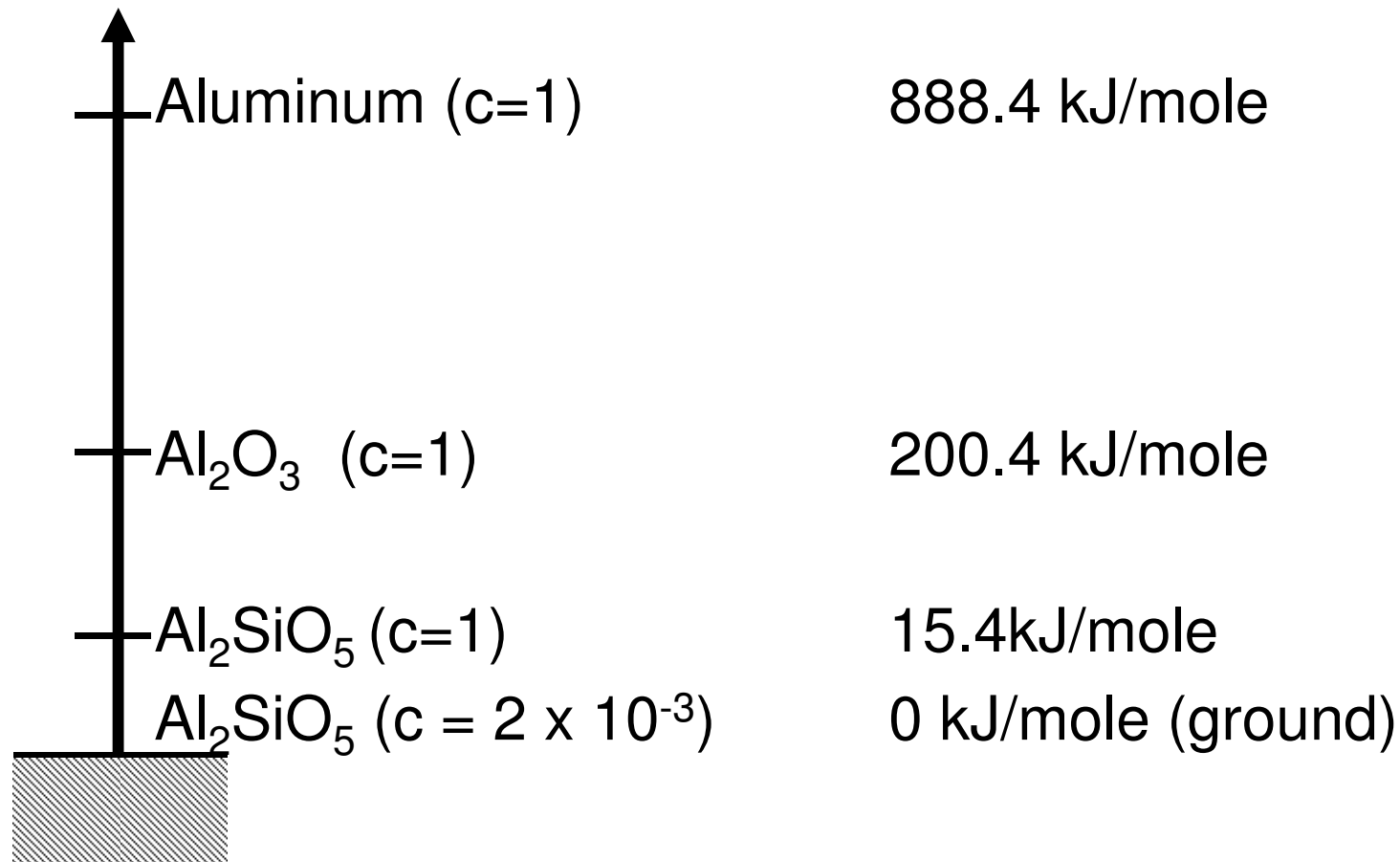
The above table is an average for clean, dry air at sea level.  
1 part/million = 0.0001 percent.

$$T_0 = 298.2 \text{ K}, P_0 = 101.3 \text{ kPA}$$

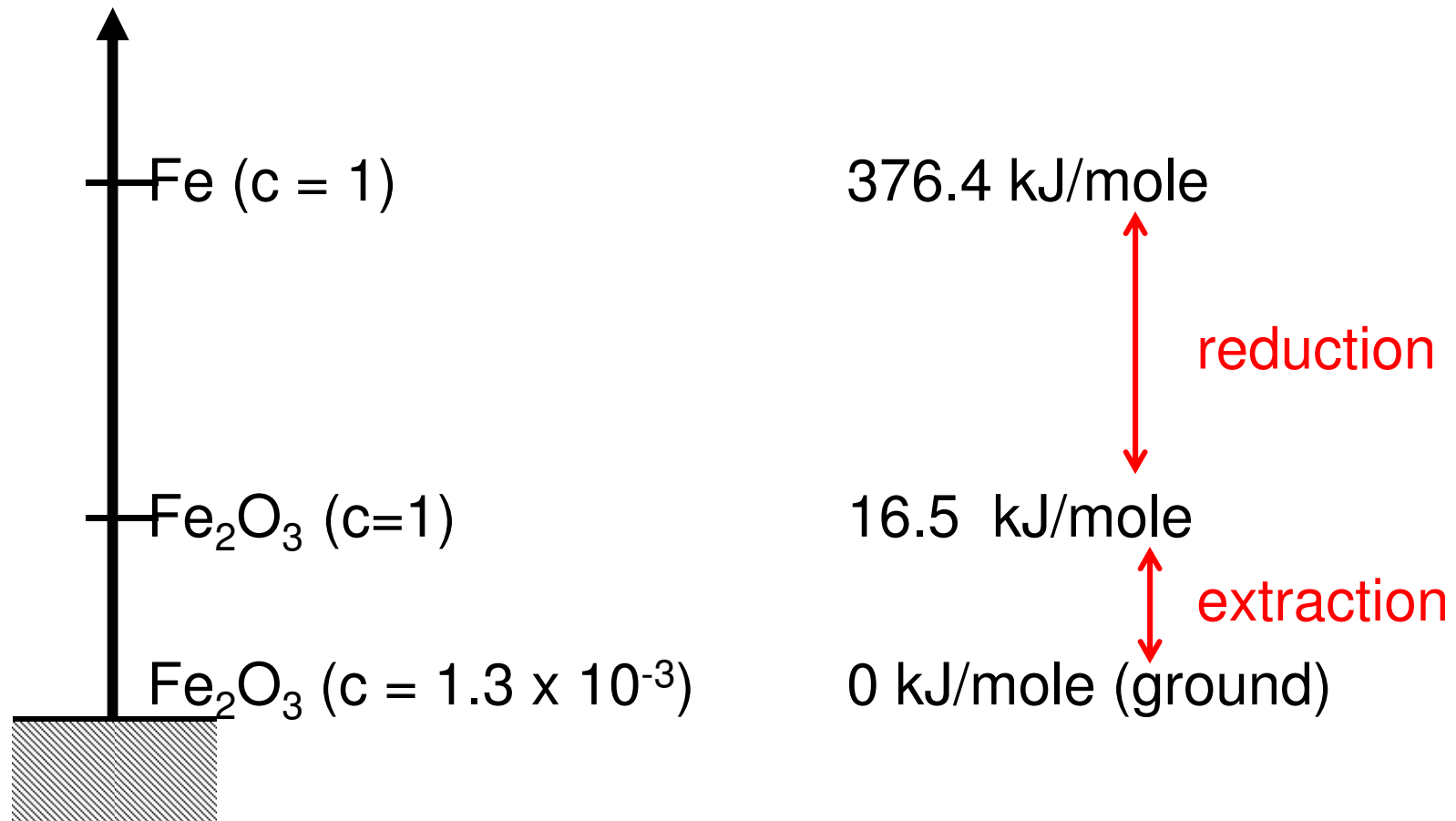
# Exergy Reference System



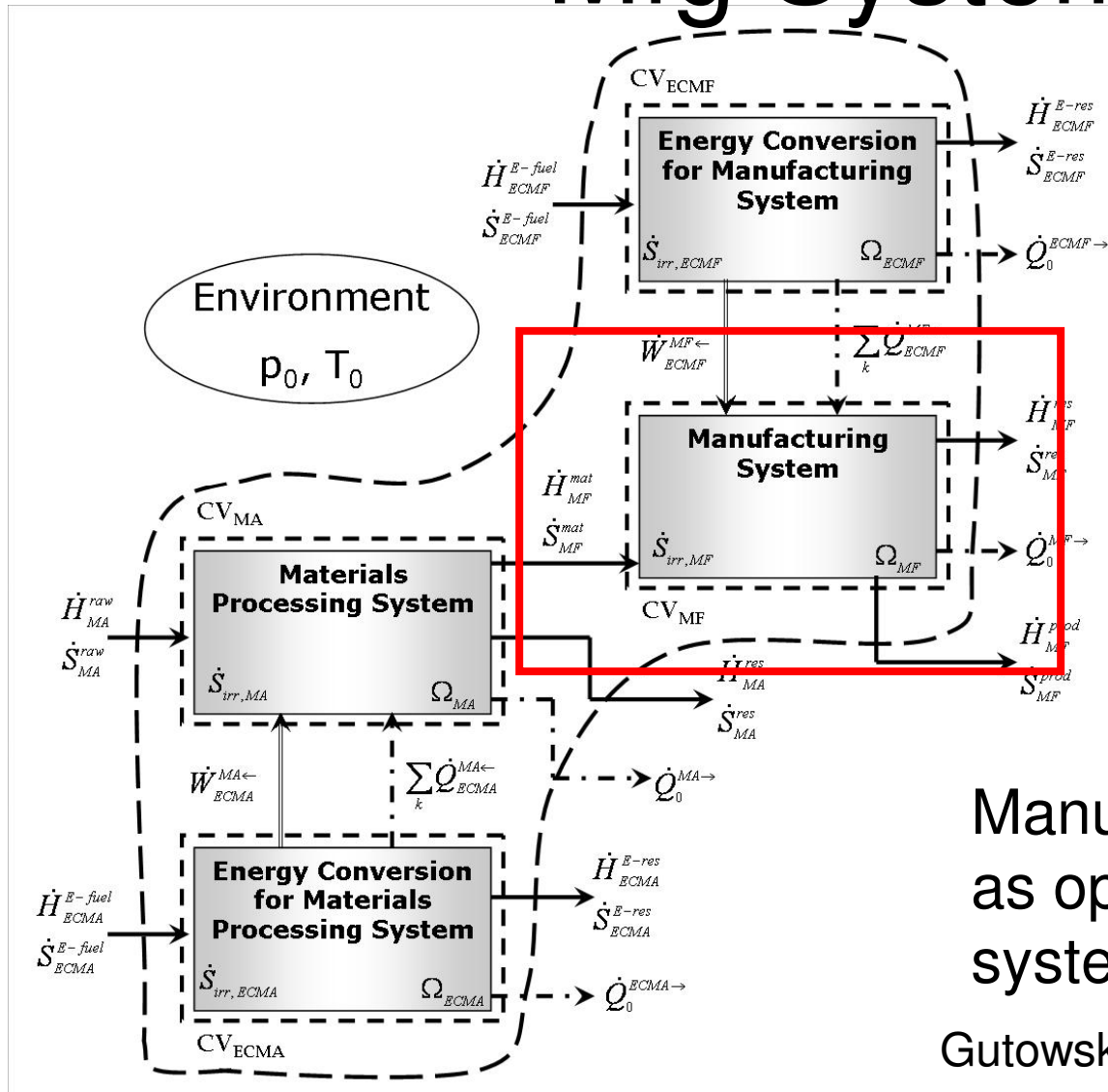
# Exergy Reference System



# Example; making pure iron from the crust



# Mfg Systems



Manufacturing Systems as open thermodynamic systems

Gutowski et al ES&T 2009

# Balances for Mfg Process

Mass

$$\frac{dm_{MF}}{dt} = \left( \sum_{i=1} \dot{N}_{i,in} M_i \right)_{MF} - \left( \sum_{i=1} \dot{N}_{i,out} M_i \right)_{MF}$$

Energy

$$\frac{dE_{MF}}{dt} = \sum_i \dot{Q}_{ECMF}^{MF \leftarrow} - \dot{Q}_0^{MF \rightarrow} + \dot{W}_{ECMF}^{MF \leftarrow} + \dot{H}_{MF}^{mat} - \dot{H}_{MF}^{prod} - \dot{H}_{MF}^{res}$$

Entropy

$$\frac{dS_{MF}}{dt} = \sum_i \frac{\dot{Q}_{ECMF}^{MF \leftarrow}}{T_i} - \frac{\dot{Q}_0^{MF \rightarrow}}{T_0} + \dot{S}_{MF}^{mat} - \dot{S}_{MF}^{prod} - \dot{S}_{MF}^{res} + \dot{S}_{irr, MF}$$

## *Work Rate for Mfg Process in Steady State*

$$\begin{aligned} \dot{W}_{ECMF}^{MF\leftarrow} &= ((\dot{H}_{MF}^{prod} + \dot{H}_{MF}^{res}) - \dot{H}_{MF}^{mat}) \\ &- T_0 ((\dot{S}_{MF}^{prod} + \dot{S}_{MF}^{res}) - \dot{S}_{MF}^{mat}) \\ &- \sum_{i>0} \left( 1 - \frac{T_0}{T_i} \right) \dot{Q}_{ECMF}^{MF\leftarrow} + T_0 \dot{S}_{irr, MF} \end{aligned}$$



# *Exergy and Work*

$$B = (H - T_o S) - (H - T_o S)_o$$

$$\dot{W}_{ECMF}^{MF\leftarrow} = ((\dot{B}_{MF}^{prod} + \dot{B}_{MF}^{res}) - \dot{B}_{MF}^{mat}) - \sum_{i>0} \left(1 - \frac{T_0}{T_i}\right) \dot{Q}_{ECMF}^{MF\leftarrow} + T_0 \dot{S}_{irr, MF}$$

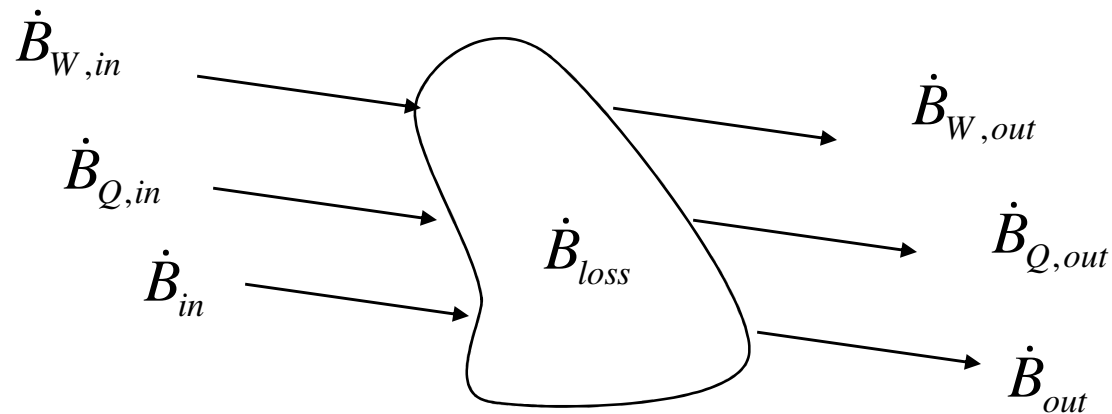
Examples: plastic work, melting, vaporizing etc.

# Physical & Chemical Exergy

$$\begin{aligned}
 \dot{W}_{ECMF}^{MF\leftarrow} = & \left( \left( \dot{B}_{MF}^{prod} + \dot{B}_{MF}^{res} \right) - \dot{B}_{MF}^{mat} \right)^{ph} \\
 & + \left( \sum_{i=1}^n b_i^{ch} \dot{N}_i \right)_{MF}^{prod} + \left( \sum_{i=1}^n b_i^{ch} \dot{N}_i \right)_{MF}^{res} - \\
 & \left( \sum_{i=1}^n b_i^{ch} \dot{N}_i \right)_{MF}^{mat} - \sum_{i>0} \left( 1 - \frac{T_0}{T_i} \right) \dot{Q}_{ECMF}^{MF\leftarrow} + T_0 \dot{S}_{irr,MF}
 \end{aligned}$$

Here all chemical exergy terms ( $b^{ch}$ ) are at  $T_o, P_o$

# Exergy Balance, Open System



$$\dot{B}_{in} + \dot{B}_{W,in} + \dot{B}_{Q,in} = \dot{B}_{out} + \dot{B}_{W,out} + \dot{B}_{Q,out} + \dot{B}_{loss}$$

*Includes: materials flows, heat and work interactions*

# *Example Calculations*

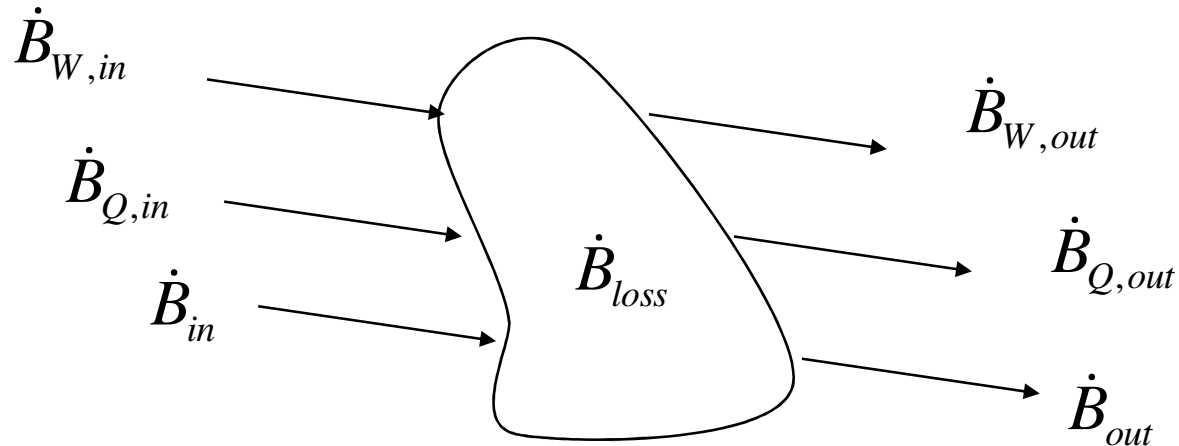
## *Second Law Efficiency*

- Melting of iron
- Machining
- CVD of SiO<sub>2</sub>
- Thermal Oxidation of SiO<sub>2</sub>
- High Pressure SWCNT

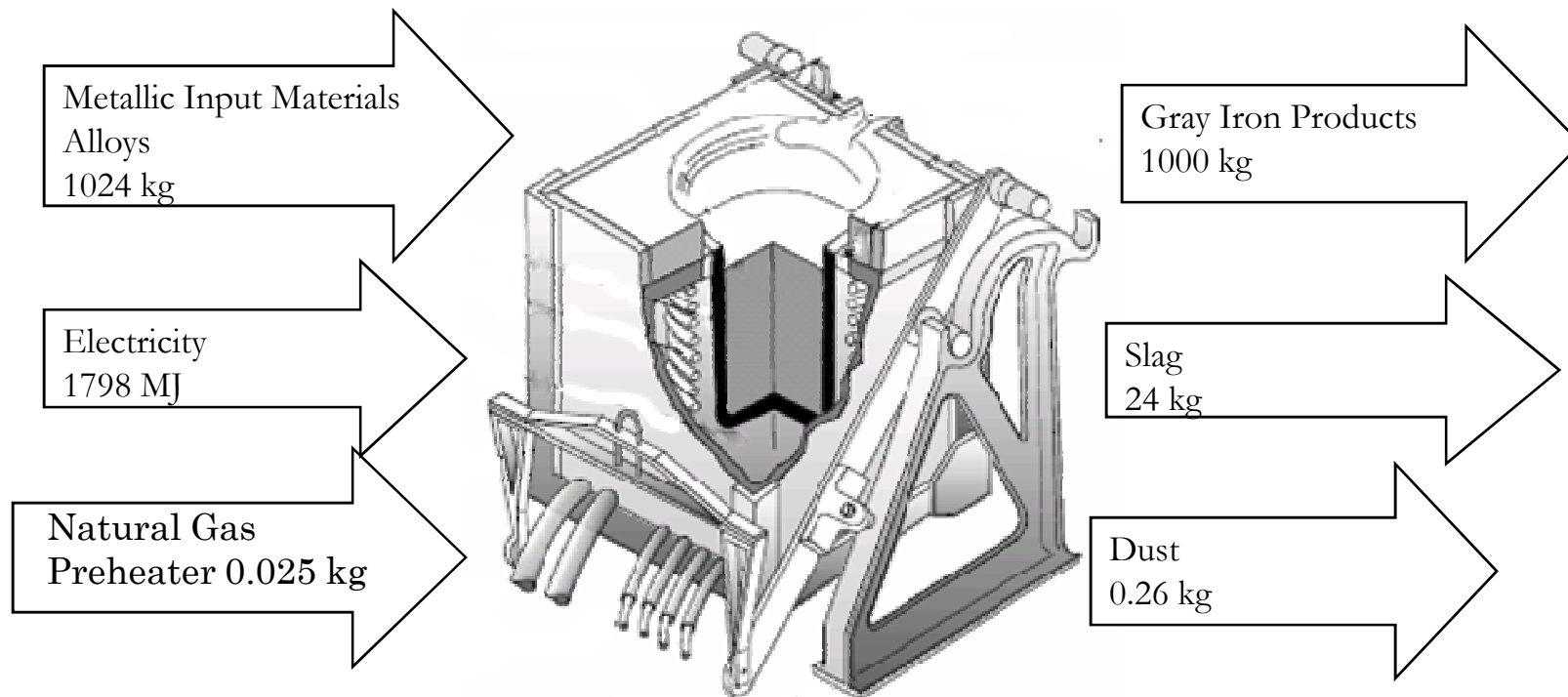
# Second Law Efficiency

$$\eta_p = \frac{B_{\text{useful output}}}{B_{\text{in}}}$$

$$\eta = \frac{W_{\text{min}}}{W_{\text{actual}}}$$



# Induction Melting Exergy Analysis



**Boundaries are drawn around the entire facility,  
all components are at standard pressure and temperature**

# *Batch Induction Melter Exergy Analysis\**

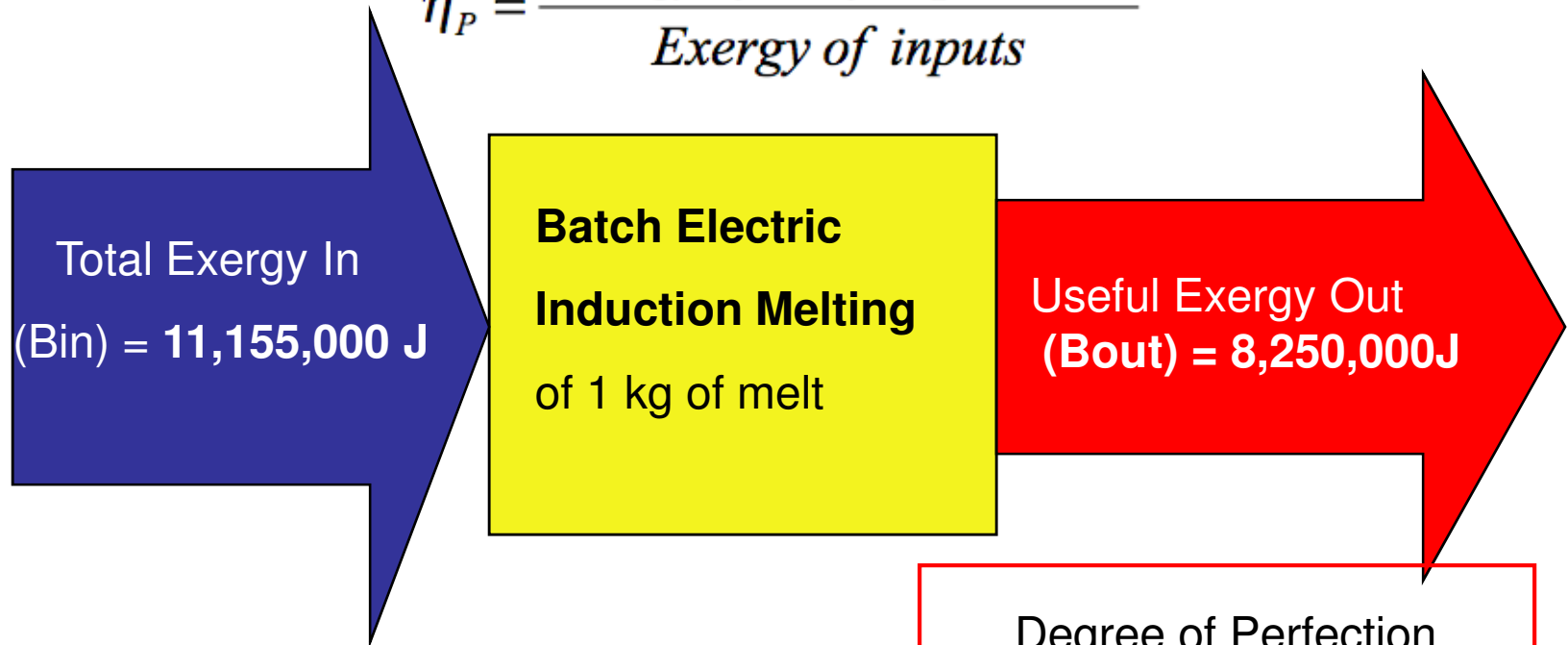
## Ductile Iron Batch Electric Induction Melting

<u>Material</u>	<u>Amount (kg)</u>	<u>Weight Percent</u>	<u>Standard Chemical Exergy (MJ/kg)</u>	<u>Exergy (MJ)</u>	<u>Percent Total Exergy</u>
<b>Input Materials</b>					
Steel Scrap	439	42.85%	6.89	3022.25	15.39%
Pig Iron	1.6	0.16%	8.18	13.43	0.07%
Ductile Iron Remelt	535	52.25%	8.44	4513.98	22.99%
65% Silicon Carbide Briquettes	4.3	0.42%	31.73	137.62	0.70%
75% Ferrosilicon	3.0	0.29%	24.51	72.46	0.37%
5% MgFeSi	14.8	1.44%	19.09	282.30	1.44%
Copper	1.7	0.17%	2.11	3.69	0.02%
Tin	0.005	0.00%	1.13	0.01	0.00%
62% Fe-Molybdenum	6.2	0.61%	7.28	45.35	0.23%
Carbon 9012	18	1.80%	34.16	628.45	3.20%
Natural Gas Preheater	0.02	0.00%	51.84	1.27	0.01%
Electricity				5418.00	55.59%
<b>Total Inputs</b>	<b>1024</b>	<b>100.00%</b>		<b>14138.83</b>	<b>100.00%</b>
<b>Output Materials</b>					
Ductile Iron Melt	1000.2	96.69%	8.44	8436.45	99.29%
Slag	33.9	3.28%	1.14	60.05	0.71%
Dust	0.3	0.02%	0.26	0.07	0.00%
<b>Total Outputs</b>	<b>1034</b>	<b>100.00%</b>		<b>8497</b>	<b>100.00%</b>
<b>Mass Difference</b>	<b>-1.05%</b>				

\*including losses at Utility

# Batch Electric Degree of Perfection

$$\eta_P = \frac{\text{Exergy of useful products}}{\text{Exergy of inputs}}$$



Component	Exergy in (J)
Metallics	8,700,000
Electricity*	1,806,000

\*not including utility losses

Degree of Perfection

$$\eta_P = \frac{8,250,000J}{10,420,000J} = 0.79$$



# Minimum work

$$dw = dh - T_o ds$$

$$dw = C dT - c dT/T$$

$$w = c(T - T_o) - T_o c \ln (T/T_o) + h_{fusion} (1 - T_o/T_m)$$

Using  $T_m = 1540\text{C}$ ,  $c = 0.67 \text{ J/gK}$  and

$$H_{fusion} = 272.15 \text{ J/g}$$

$$w_{min} = 889 \text{ J/g} = 0.9 \text{ MJ/kg}$$

$$w_{actual} = 5.4 \text{ MJ/kg} / 3 = 1.8 \text{ MJ/kg}$$

$$\eta = 0.9 / 1.8 = 50\%$$

# Machining

## Leaded Steel and the Real Area of Contact in Metal Cutting

By M. C. SHAW, P. A. SMITH, N. H. COOK, AND E. G. LOEWEN

The action of lead in free-machining steel is discussed and the thickness of the layer of lead responsible for the improved lubrication between chip and tool is found to be extremely thin. Measurements made on the same steel with and without lead present enable the real area of contact between chip and tool to be estimated and this is found to be between 1 and 2 per cent of the apparent area of contact. The cutting characteristics of steel containing lead are compared with those for steel without lead as well as those for pure lead. It is found that the presence of lead makes effective fluids such as carbon tetrachloride less sensitive to an increase in cutting speed.

(Taken from *Transactions of the ASME*, July, 1957)

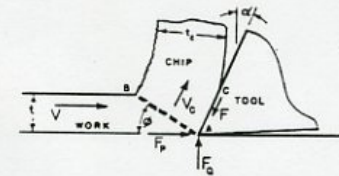


FIG. 1 CONDITIONS AT POINT OF CUTTING TOOL DURING CONTINUOUS CUTTING. WIDTH OF CUT ALONG CUTTING EDGE =  $b$



FIG. 2 ACTUAL SURFACES IN CONTACT AT VERY HIGH MAGNIFICATION

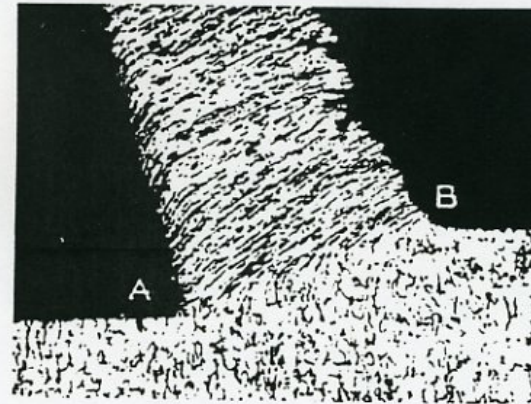
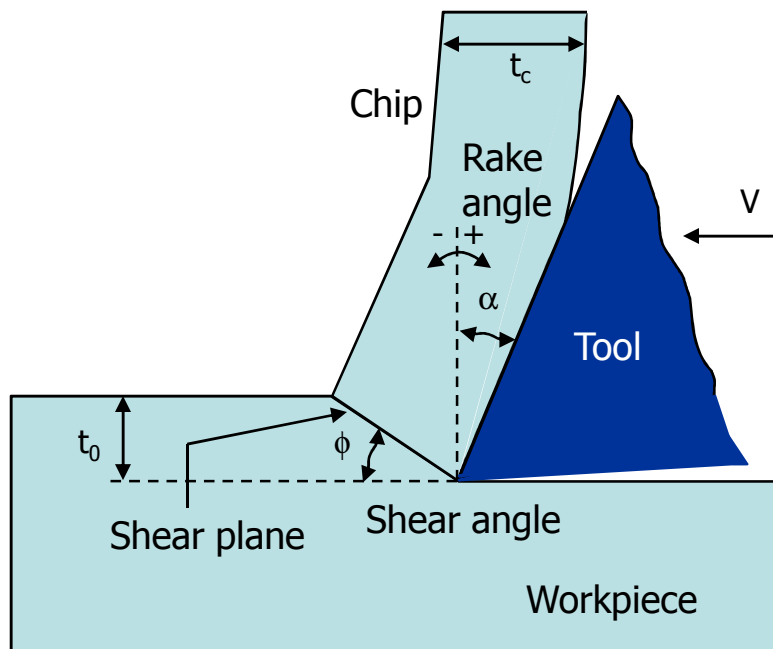


Fig. 1. In the process of metal cutting, tool tip, A, produces chips above the line AB with no deformation of the metal below this line.

QuickTime™ and a decompressor are needed to see this picture.

# Basic Machining Mechanism



$$F \cdot V = \text{Power} = \frac{d(\text{work})}{dt} = \dot{\text{work}}$$

$$\frac{\dot{\text{work}}}{\dot{\text{vol}}} = \text{specific energy} = u_s$$

$$u_s = u_{\text{plastic work}} \text{ (65 to 80\%)} + u_{\text{friction}}$$

$$u_p = \int \bar{\sigma} d\bar{\epsilon} \cong \tau\gamma \quad 2 \leq \gamma \leq 4$$

$$u_p \cong \tau\gamma \cong \frac{1}{6} H \times (2 - 4)$$

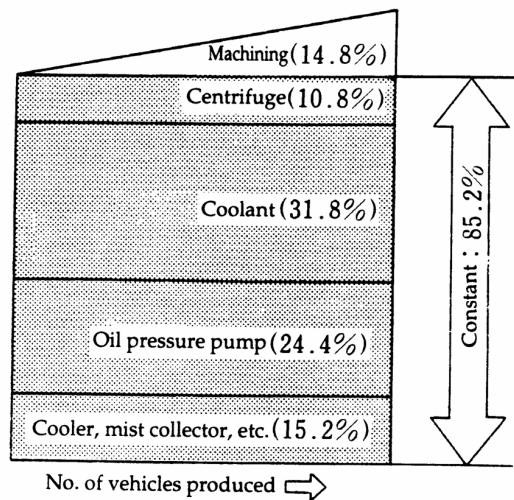
Approximation

$$u_s \sim H \text{ (Hardness)}$$

## Results are in terms of primary energy

	Production Machining Center (2000)		Manual Milling Machine (1985)	
<b>Electricity Breakdown</b>				
Constant start-up operations (idle)	85.2%		31.6%	
Run-time operations (positioning, loading, etc)	3.5%		0% (manual)	
Material removal operations (in cut)	11.3%		69.4%	
<b>Electricity Requirements</b>				
Constant start-up operations (idle)	166 kW		0.7 kW	
Run-time operations (positioning, loading, etc)	6.8 kW		0 kW	
Material removal operations (in cut)	22 kW		2.1 kW	
<b>Machine Use Scenario</b>				
Arbitrary Number of work hours	1000 hours		1000 hours	
Machine uptime	90%		90%	
Machine hours (idle, positioning, or in cut)	900 hours		900 hours	
Percentage of machine hours spent idle	10%		65%	
Machine hours spent idle	90 hours		585 hours	
Active machine hours per 1000 work hours	810 hours		315 hours	
<b>Machining Scenario</b>				
Percentage of machine hours spent positioning	30%		70%	
Machine hours spent positioning	243 hours		221 hours	
Percentage of machine hours spent in cut	70%		30%	
Machine hours spent in cut	567 hours		94.5 hours	
<b>Electricity Use per 1000 work hours</b>				
Constant start-up operations (idle)	149288 kWh		600 kWh	
Run-time operations (positioning, loading, etc)	5471 kWh		0 kWh	
Material removal operations (in cut)	6237 kWh		100 kWh	
Total electricity use per 1000 work hours	160996 kWh		700 kWh	
<b>Electricity Used per Material Removed</b>				
Material Machined	Aluminum	Steel	Aluminum	Steel
Material Removal Rate	20.0 cm <sup>3</sup> /sec	4.7 cm <sup>3</sup> /sec	1.5 cm <sup>3</sup> /sec	0.35 cm <sup>3</sup> /sec
Material removed per 1000 work hours	40824000 cm <sup>3</sup>	9593640 cm <sup>3</sup>	510300 cm <sup>3</sup>	119070 cm <sup>3</sup>
<b>Electricity used/Material removed</b>	<b>14.2 kJ/cm<sup>3</sup></b>	<b>60 kJ/cm<sup>3</sup></b>	<b>4.9 kJ/cm<sup>3</sup></b>	<b>21 kJ/cm<sup>3</sup></b>

# Production machining energy Vs production rate



**Figure 3.3 Energy Use Breakdown by Type**

**TABLE 21.2**

**Approximate Range of Energy Requirements in Cutting Operations at the Drive Motor of the Machine Tool (for Dull Tools, Multiply by 1.25)**

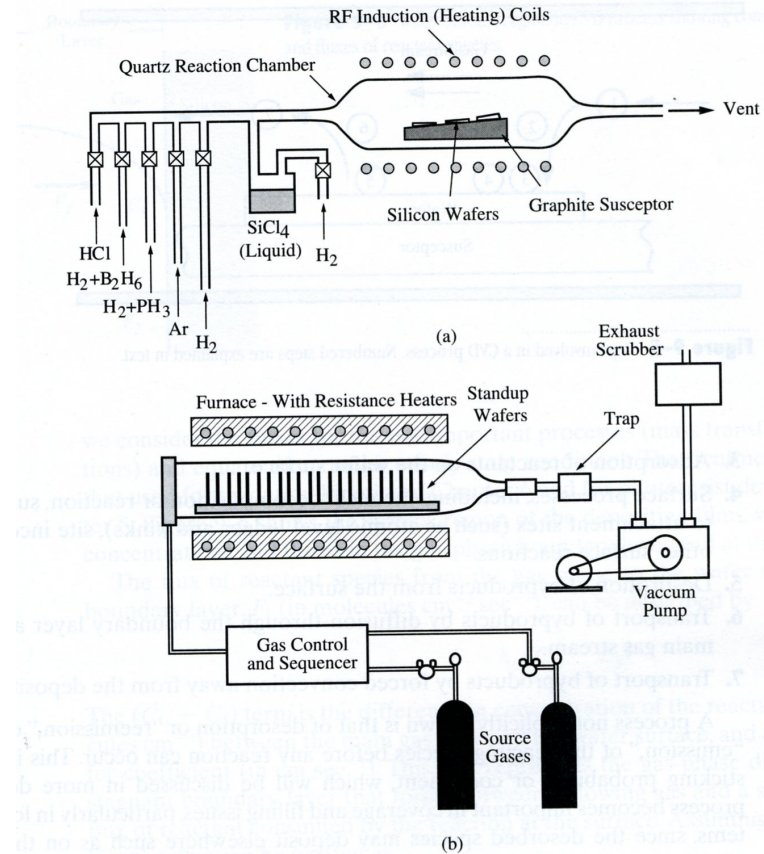
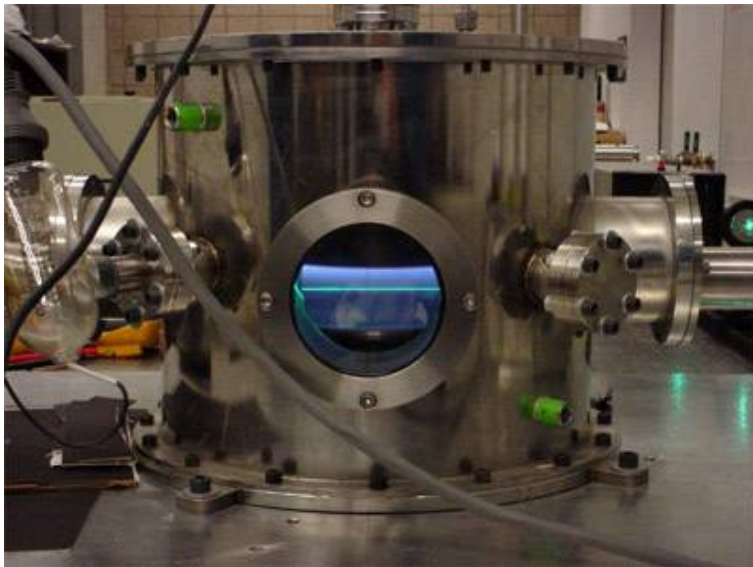
Material	Specific energy	
	W · s/mm <sup>3</sup>	hp · min/in <sup>3</sup>
Aluminum alloys	0.4–1	0.15–0.4
Cast irons	1.1–5.4	0.4–2
Copper alloys	1.4–3.2	0.5–1.2
High-temperature alloys	3.2–8	1.2–3
Magnesium alloys	0.3–0.6	0.1–0.2
Nickel alloys	4.8–6.7	1.8–2.5
Refractory alloys	3–9	1.1–3.5
Stainless steels	2–5	0.8–1.9
Steels	2–9	0.7–3.4
Titanium alloys	2–5	0.7–2

$$\eta = W_{\min} / u_s \approx 0.5,$$

Production machining of Aluminum,  $\eta = 0.35 / 14.2 / 3 = 7.5\%$

Manual machining of aluminum,  $\eta = 0.35 / 4.9 / 3 = 21\%$

# Plasma Enhanced Chemical Vapor Deposition (CVD)



**Figure 9-4** Chemical Vapor Deposition (CVD) systems. (a) is an atmospheric cold-wall system used for deposition of epitaxial silicon. (b) is a low-pressure hot-wall system used for deposition of polycrystalline and amorphous films, such as polysilicon and silicon dioxide, respectively.

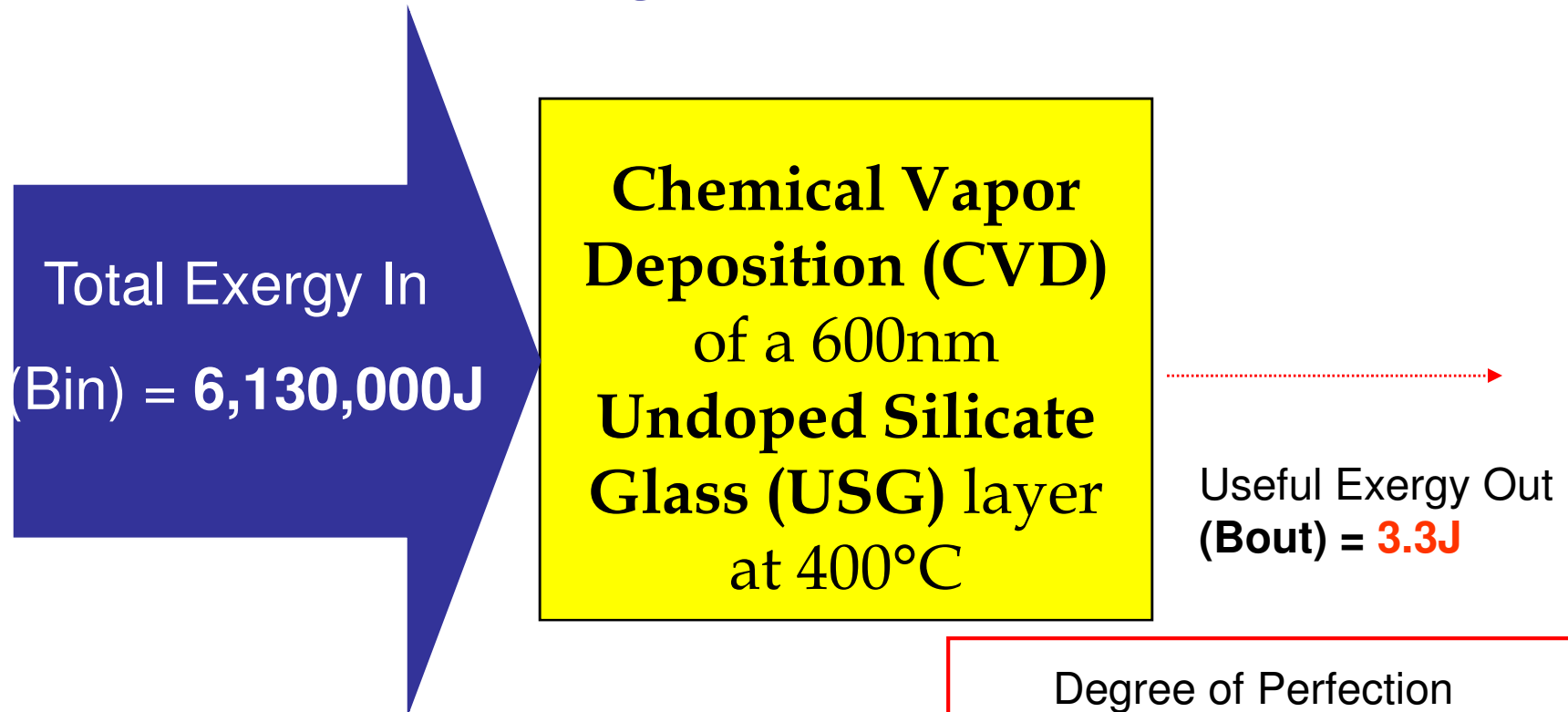
# Plasma enhanced CVD

<b>Input Deposition Gases</b>				
<i>Species</i>	<i>Input mass (g)</i>	<i>Input moles or primary energy</i>	<i>Exergy (J)</i>	<i>%Total Inputs</i>
SiH4	0.95	0.029579mol	40928.6	<b>0.749</b>
O2	0.49	0.015313mol	60.79	
Ar	0.34	0.008511mol	99.5	
N2	196.9	7.028779mol	4849.9	

<b>Input Cleaning Gases</b>				
CH4	69.41	4.326643mol	3598253	<b>63.0</b>
NF3	31.06	0.437453mol	266931.6	
<b>Input Energy</b>				
Electricity		2220000J	2220000	<b>36.2</b>

<b>Outputs</b>				
Undoped Silicate Glass laye	0.0248	0.000414mol	3.2667	

# CVD Degree of Perfection



Component	Exergy in (J)
Input Gases	45,900
Cleaning Gases	3,865,000
Electricity*	2,220,000

\*not including utility losses

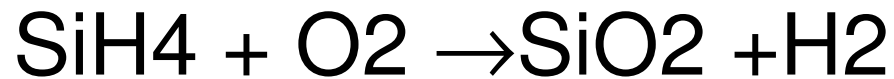
Degree of Perfection

$$\eta_P = \frac{3.267J}{6,131,123J} = 5.33 * 10^{-7}$$

Data from Sarah Boyd et. al. (2006)



# CVD deposition of SiO<sub>2</sub> glass



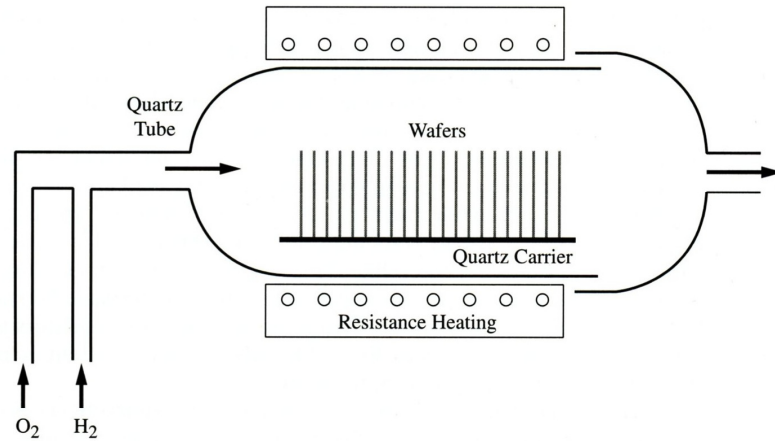
$$1383.7 + 3.97 - 7.9 + 2 \times 236.1 = 907.6 \text{ kJ/mol SiO}_2$$

$$907.6 \text{ kJ/mol} \times 1 \text{ mol/60g} \times 1000\text{g/kg} = 15\text{MJ/kg}$$

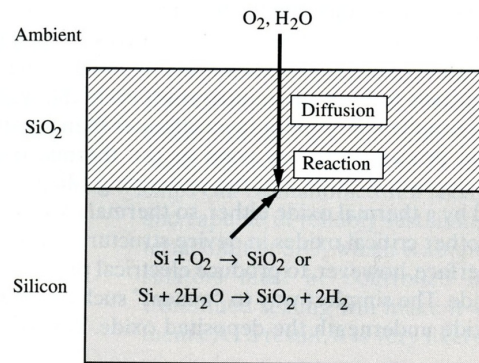
$$\text{Actual electricity} = 2.2 \text{ MJ/0.0248 g} \Rightarrow 88.7 \text{ GJ/kg}$$

$$\eta = 15.13/88,700 = 1.7 \times 10^{-4}$$

# Thermal Oxidation



**Figure 6-7** Conceptual silicon oxidation system.



**Figure 6-2** Basic process for the oxidation of silicon. The chemical reaction takes place at the  $Si/SiO_2$  interface.



# Wet Oxidation Process

<b>Input Gases</b>				
<i>Species</i>	<i>Input mass (g)</i>	<i>Input moles or energy (J)</i>	<i>Exergy (J)</i>	<i>%Total Input Exergy</i>
N2	54.069	1.9301	1331.769	0.00089
O2	6.1399	0.19188	761.7636	0.00051
H2	0.4479	0.22218	52456.7	0.0351
<b>Silicon Consumed from Substrate</b>				
Si	0.03091	0.001101	940.54	0.00063
<b>Input Energy</b>				
Electricity		149256000	149256000	0.99963

<b>Outputs</b>				
SiO2 layer	0.066253	0.001103	8.711	

*degree of perfection*

$$\eta_p = 5.83 \cdot 10^{-8}$$

<b>Sputtering of an AlCu film (Full Process)</b>				
<b>Input Materials</b>				
<i>Inputs</i>	<i>Mass (g)</i>	<i>Moles</i>	<i>Specific Chemical Exergy (kJ/mol)</i>	<i>Exergy (kJ)</i>
Ar	3.43	0.09	11.69	1.00
AlCu	2.44	0.09	885.0	78.96
<b>Input Energy</b>				
Electricity				29909
<i>Total In</i>				29988
<b>Output</b>				
AlCu Film	0.498	1.82E-02	885.04	16.13
<i>Total Out</i>				16.13
<b>Degree of Perfection (<math>\rho</math>)</b>				5.38E-04

<b>Dry Etching of a Silicon Nitride Film (Full Process)</b>				
<b>Input Materials</b>				
<i>Inputs</i>	<i>Mass (g)</i>	<i>Moles</i>	<i>Specific Chemical Exergy (kJ/mol)</i>	<i>Exergy (kJ)</i>
He	2.46E-02	6.13E-03	30.37	1.86E-01
SF <sub>6</sub>	2.688	1.84E-02	281.8	5.2
<b>Input Energy</b>				
Electricity				1178
<i>Total In</i>				1184
<b>Output</b>				
Etched Si <sub>3</sub> N <sub>4</sub>	0.033	2.34E-04	1917.88	0.45
<i>Total Out</i>				0.45
<b>Exergetic Efficiency of Removal (<math>\rho</math>)</b>				3.79E-04

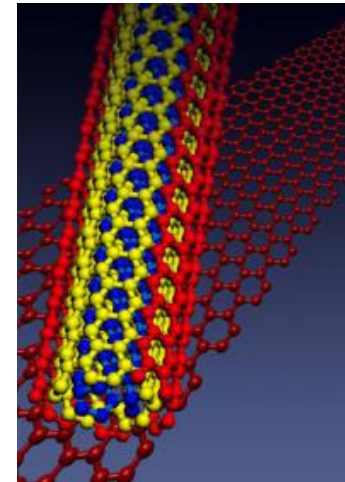
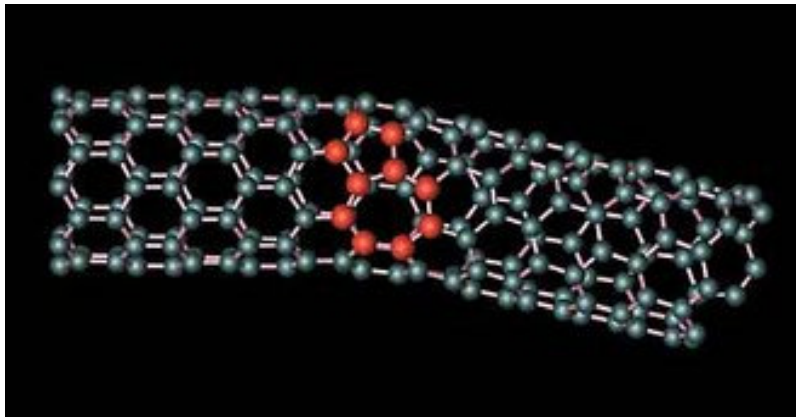
<b>Wet Etching of a Silicon Nitride Film (Etch Only)</b>				
<b>Input Materials</b>				
<i>Inputs</i>	<i>Mass (g)</i>	<i>Moles</i>	<i>Specific Chemical Exergy (kJ/mol)</i>	<i>Exergy (kJ)</i>
H <sub>3</sub> PO <sub>4</sub>	252.82	2.58	104.00	268.32
H <sub>2</sub> O	72.432	4.02	0.90	3.62
<b>Input Energy</b>				
Electricity				525.6
<i>Total In</i>				797.5
<b>Output</b>				
Etched Si <sub>3</sub> N <sub>4</sub>	0.301	2.15E-03	1917.88	4.12
<i>Total Out</i>				4.12
<b>Exergetic Efficiency of Removal (<math>\rho</math>)</b>				5.14E-03

*Data taken from  
MEMS facility*

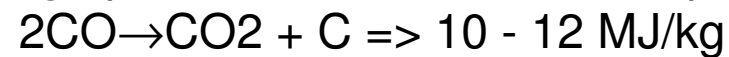
Degree of Perfection  
depends upon exergy of  
output  
Note some are removal  
processes

Tables from  
Matthew Branham  
MS thesis 2008

# Production of Carbon SWNT



Production by high pressure carbon monoxide process “HiPCO”



Estimates of electricity inputs  $\sim 30 \text{ GJ/kg}$ ,  $\eta = 12/30,000 = 0.04\%$

# Summary for $\eta_P$ ; $\eta$

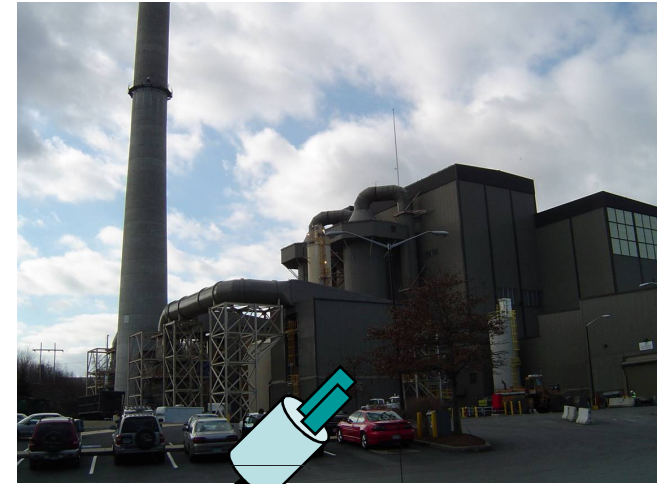
- Heating & Melting  $\sim 0.5$ ;  $0.5$
- Machining  $\sim 0.05$ ;  $0.05$  to  $0.5$  compared to  $u_s$
- Grinding  $\sim 0.005$
- Sputter, Wet and Dry Etching  $\sim 5 \times 10^{-4}$
- PECVD (SiO<sub>2</sub>)  $\sim 10^{-6}$  ;  $10^{-4}$
- Wet Oxidation  $\sim 10^{-8}$ ; (potentially negative)
- SWCNT  $\sim \underline{\hspace{1cm}}$ ;  $4 \times 10^{-4}$

# Comments

- These can be quite sensitive to rate when idle power is high
- Transit Exergy for melting processes
- Exergy of Auxiliary materials: etching, cleaning, pollution abatement, abrasive waterjet
- Also affected by exergy of the output

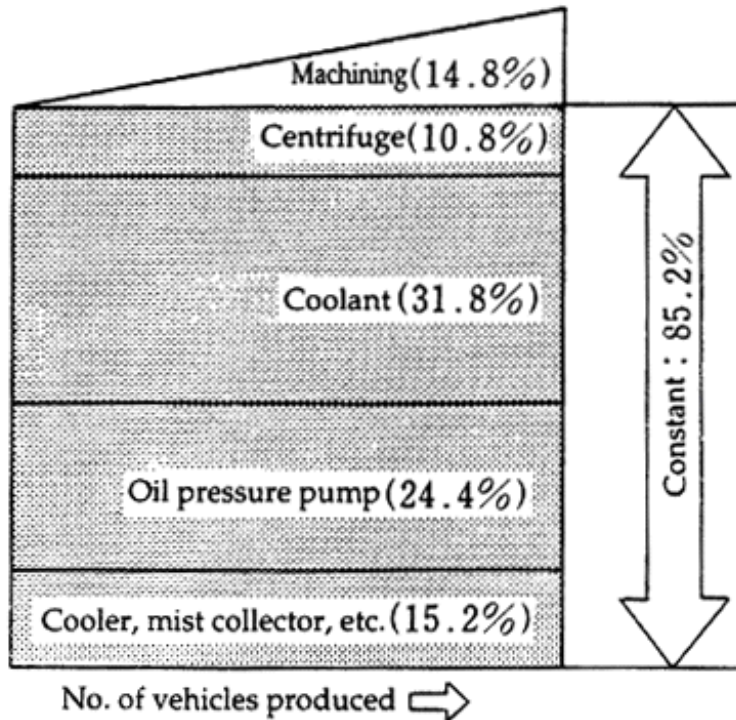
# *Energy (Electricity) Only*

1. Machining
2. Grinding
3. Casting
4. Injection Molding
5. Abrasive Waterjet
6. EDM
7. Laser DMD
8. CVD
9. Sputtering
10. Thermal Oxidation



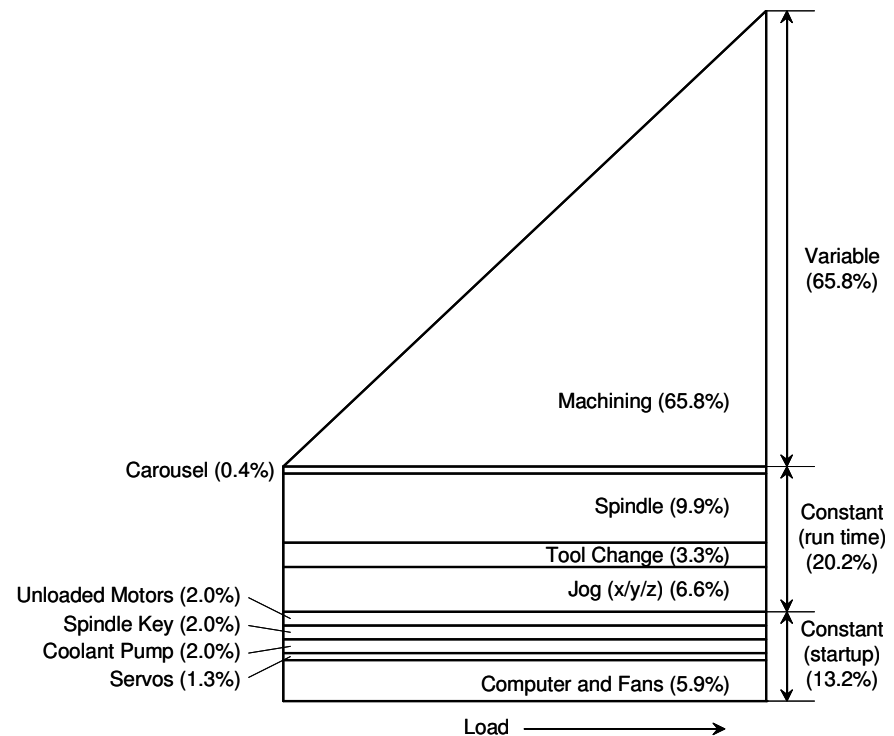


# Energy Requirements at the Machine Tool



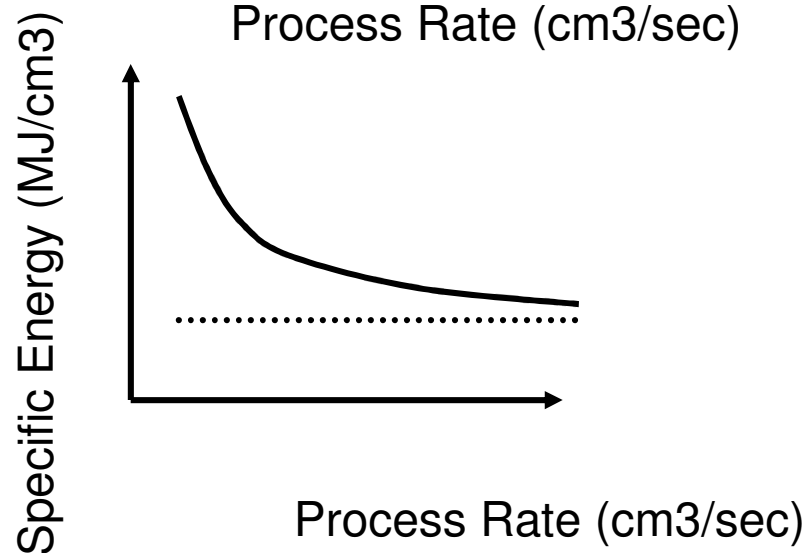
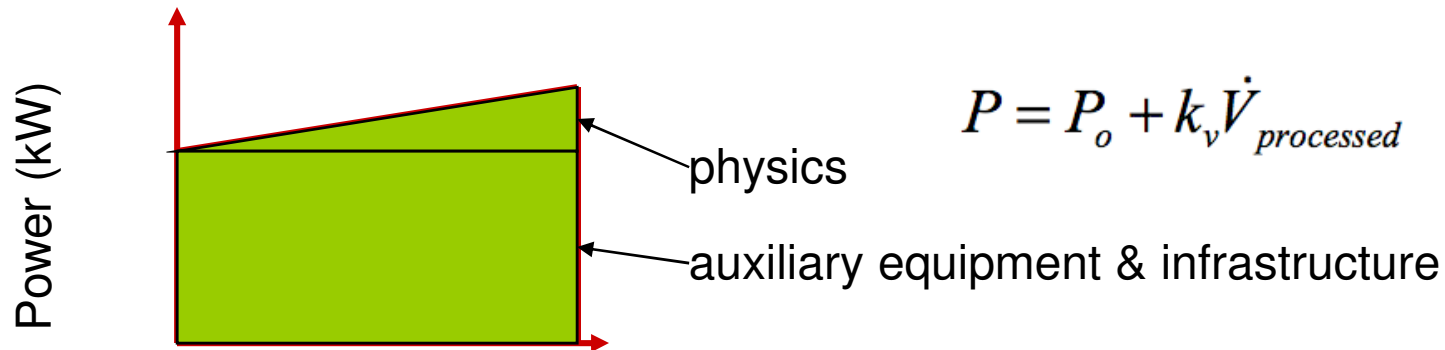
**Energy Use Breakdown by Type**

Production Machining Center



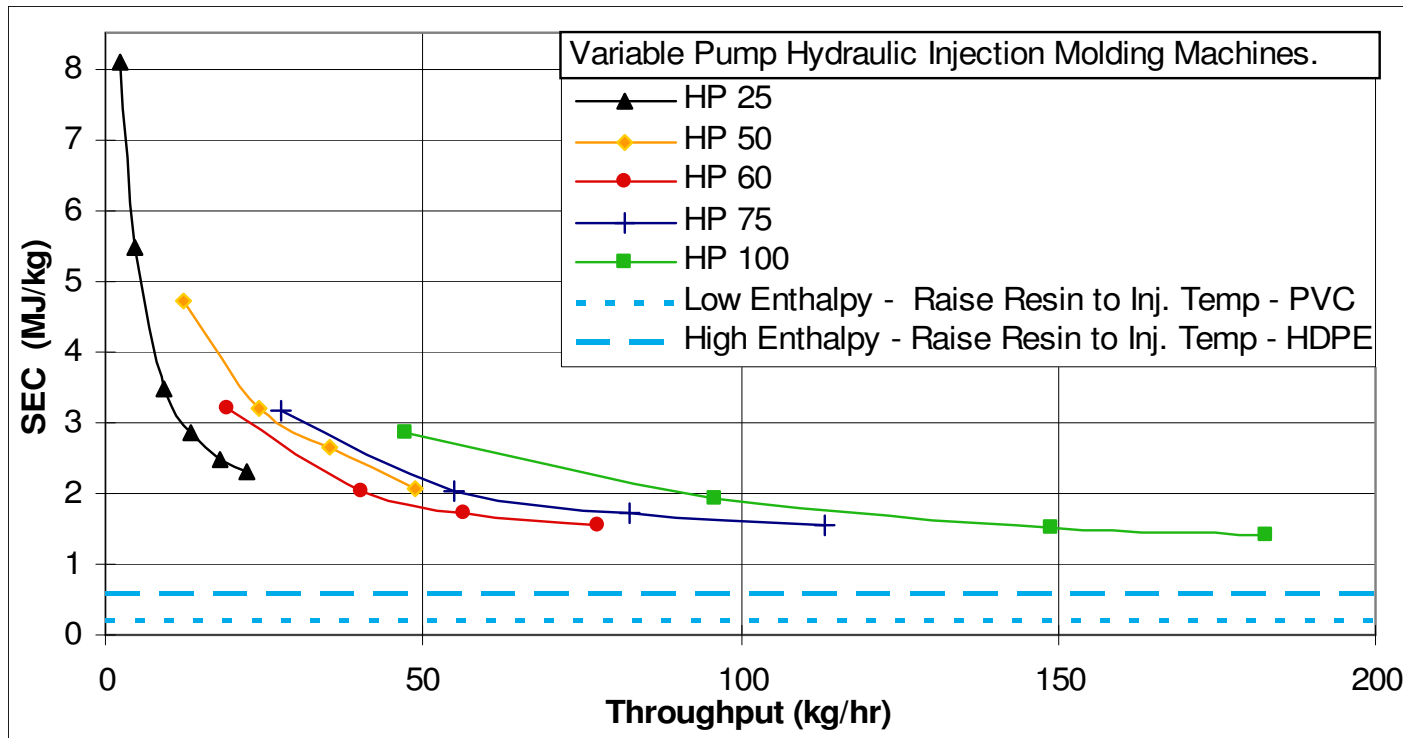
Automated Milling Machine

# *Electric Energy Intensity for Manufacturing Processes*



$$\frac{P}{\dot{V}} = \frac{P_o}{\dot{V}} + k_v = \frac{E}{V}$$

# Injection Molding Machines



Source: [Thiriez '06]

$$\frac{P}{\dot{m}} = \frac{P_o}{\dot{m}} + k_m = \frac{E}{m}$$

Does not account for the electric grid.

# Thermal Oxidation, $\text{SiO}_2$

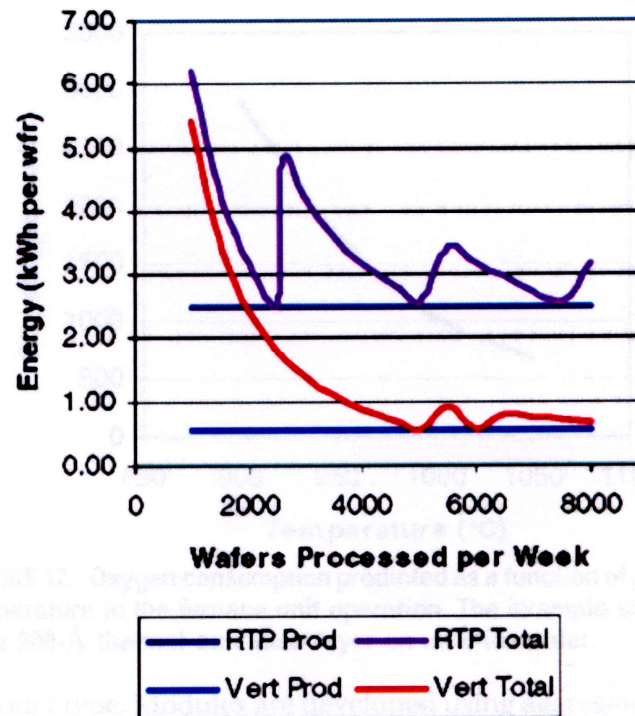


FIGURE 9. Energy consumption for growth of a 25-Å oxide layer as a function of equipment type (RTP vs vertical furnace), number of wafers processed per week, and total run time (production plus idle). The example shown is for 8-in. wafers.

Ref: Murphy et al  
es&t 2003

# Power Requirements

**TABLE 2. Average Number of Functions, Throughputs, and Power Requirements for a Hypothetical 0.13- $\mu\text{M}$  Microprocessor Wafer Fab**

unit operation	no. of functions		wafers/ run	wafers/ h	power (kW)	
	8-layer metal	6-layer metal			process	idle
implant	16	16	25	20	27	15
CVD	13	11	10	15	16	14
wafer clean	35	31	50	150	8	7.5
furnace	21	17	150	35	21	16
furnace (RTP)	7	7	1	10	48	45
photo (stepper)	27	23	1	60	115	48
photo (coater)	27	23	1	60	90	37
etch (pattern)	24	20	1	35	135	30
etch (ash)	27	23	1	20	1	0.8
metallization	11	9	1	25	150	83
CMP	18	14	1	25	29	8

Ref: Murphy et al  
es&t 2003

Process Name	Power Required		Process Rate			Electricity Required			References	
	kW		cm <sup>3</sup> /s			J/cm <sup>3</sup>				
Injection Molding	10.76	- 71.40	3.76	-	50.45	of polymer processed	1.75E+03	-	3.41E+03	[Thiriez 2006]
Machining	2.80	- 194.80	0.35	-	20.00	of material removed	3.50E+03	-	1.87E+05	[Dahmus 2004], [Morrow, Qi & Skerlos 2004] & [Time Estimation Booklet 1996]
Finish Machining	9.59		2.05E-03			of material removed	4.68E+06			[Morrow, Qi & Skerlos 2004] & [Time Estimation Booklet 1996]
CVD	14.78	- 25.00	6.54E-05	-	3.24E-03	of material deposited on wafer area	4.63E+06	-	2.44E+08	[Murphy et al. 2003], [Wolf & Tauber 1986, p.170], [Novellus Concept One 1995b] & [Krishnan Communication 2005]
Sputtering	5.04	- 19.50	1.05E-05	-	6.70E-04	of material deposited on wafer area	7.52E+06	-	6.45E+08	[Wolf & Tauber 1986] & [Holland Interview]
Grinding	7.50	- 0.03	1.66E-02	-	2.85E-02	of material removed	6.92E+04	-	3.08E+05	[Baniszewski 2005] & [Chryssolouris 1991]
Waterjet	8.16	- 16.00	5.15E-03	-	8.01E-02	of material removed	2.06E+05	-	3.66E+06	[Kurd 2004]
Wire EDM	6.60	- 14.25	2.23E-03	-	2.71E-03	of material removed	2.44E+06	-	6.39E+06	[Sodick], [Kalpakjian & Schmid 2001], & [AccuteX 2005]
Drill EDM	2.63		1.70E-07			of material removed	1.54E+10			[King Edm 2005] & [McGeough, J.A. 1988]
Laser DMD	80.00		1.28E-03			of material removed	6.24E+07			[Morrow, Qi & Skerlos 2004]
Thermal Oxidation	21.00	- 48.00	4.36E-07	-	8.18E-07	of material deposited on wafer area	2.57E+10	-	1.10E+11	[Murphy et al. 2003]

*In General, over many  
manufacturing processes,*

Idle Power

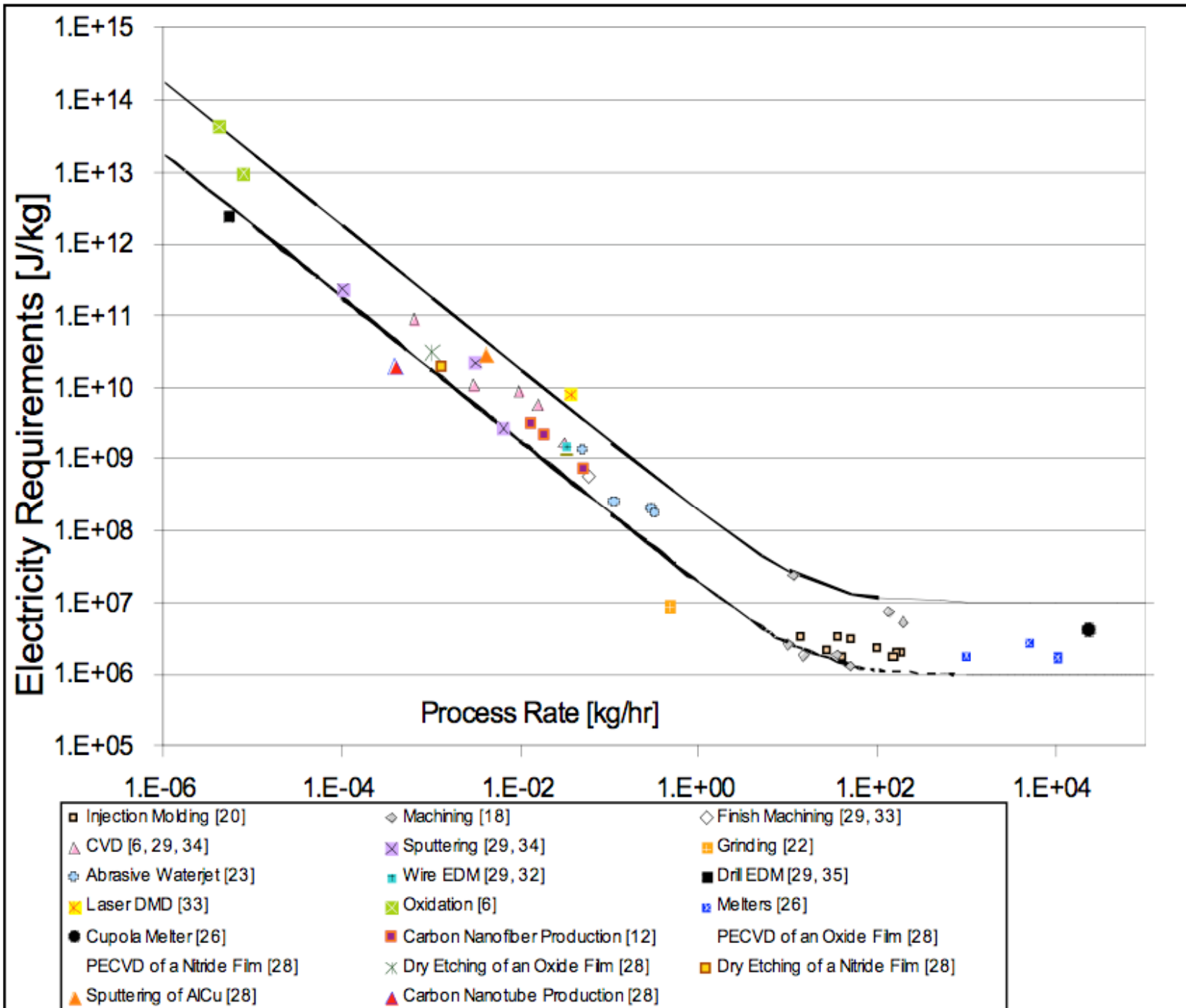
$$5kW \leq P_o \leq 50kW$$

and

Material Process Rates

$$10^{-7} \text{ cm}^3/\text{sec} \leq \dot{V} \leq 1 \text{ cm}^3/\text{sec}$$







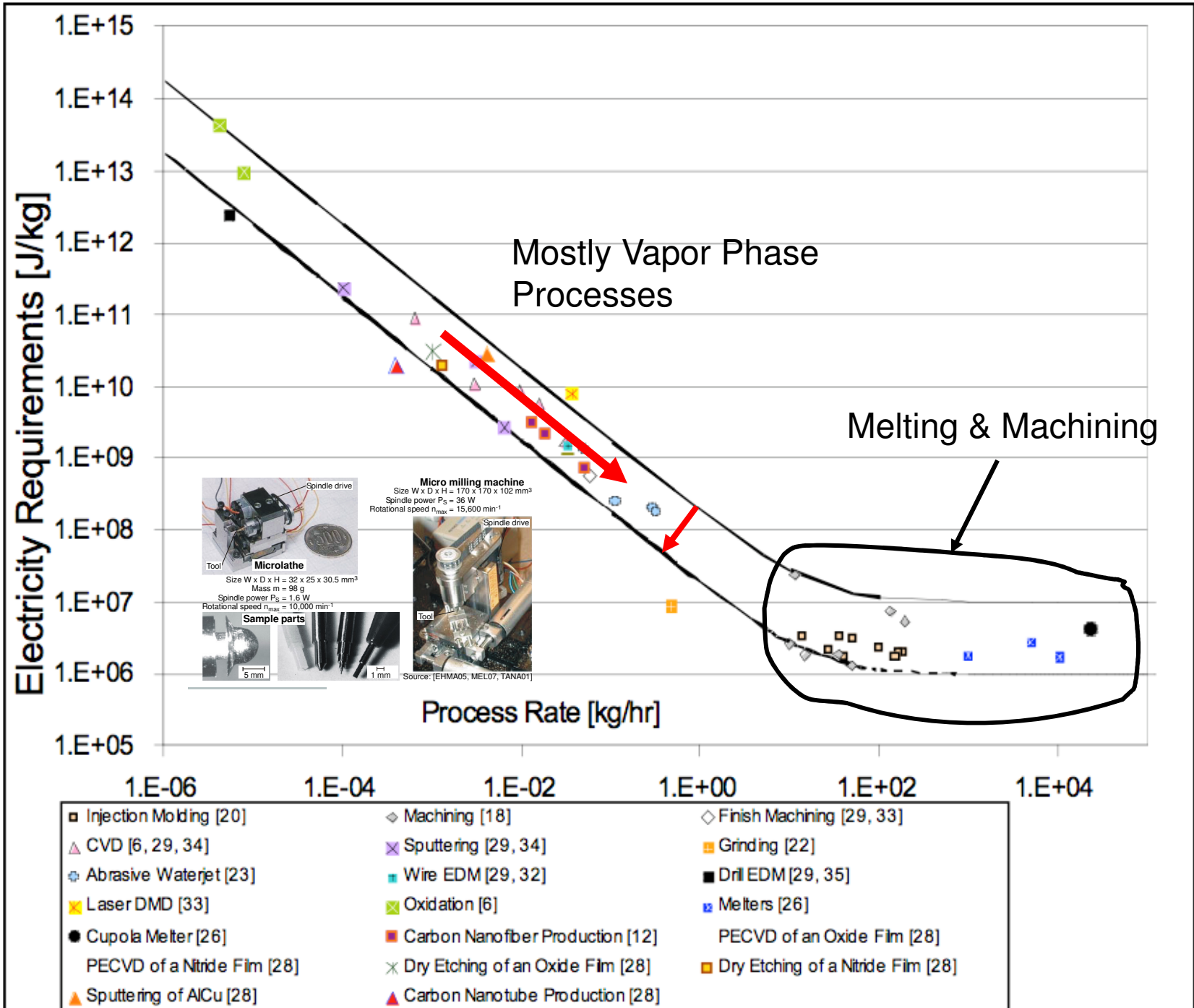
## *Why are these energy intensities so high?*

- demand for small devices, prices for energy & materials stable/declining
- vapor phase processes with slow deposition rates
- efficiency used to enhance performance, not to downsize equipment
- However, the trajectory of individual processes is usually toward faster rates and lower energy intensities

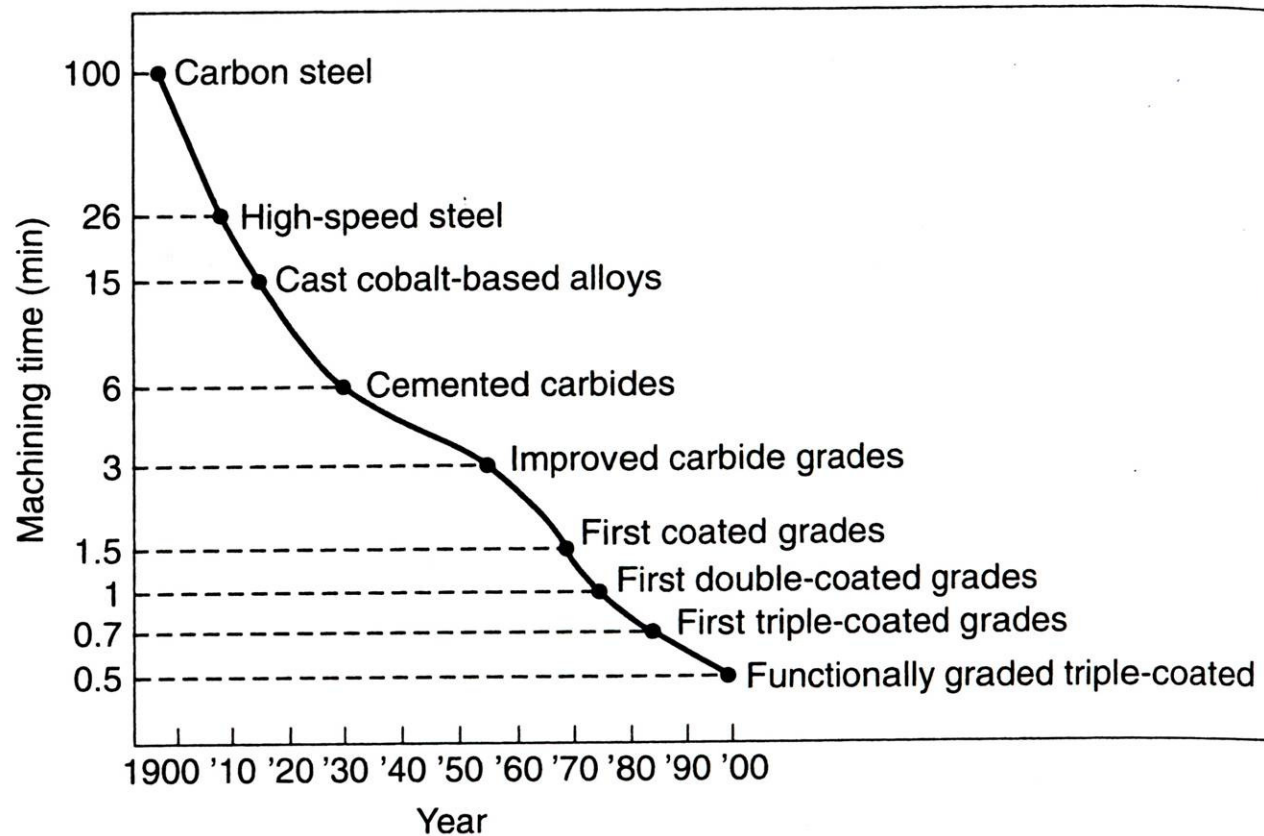
## *Keep in Mind*

- This is intensity not total used
- This is at the process, not cumulative exergy!
  - loses at energy conversion not included
  - investment into materials not included
  - infrastructure not included

*How to Improve energy  
performance of mfg processes*

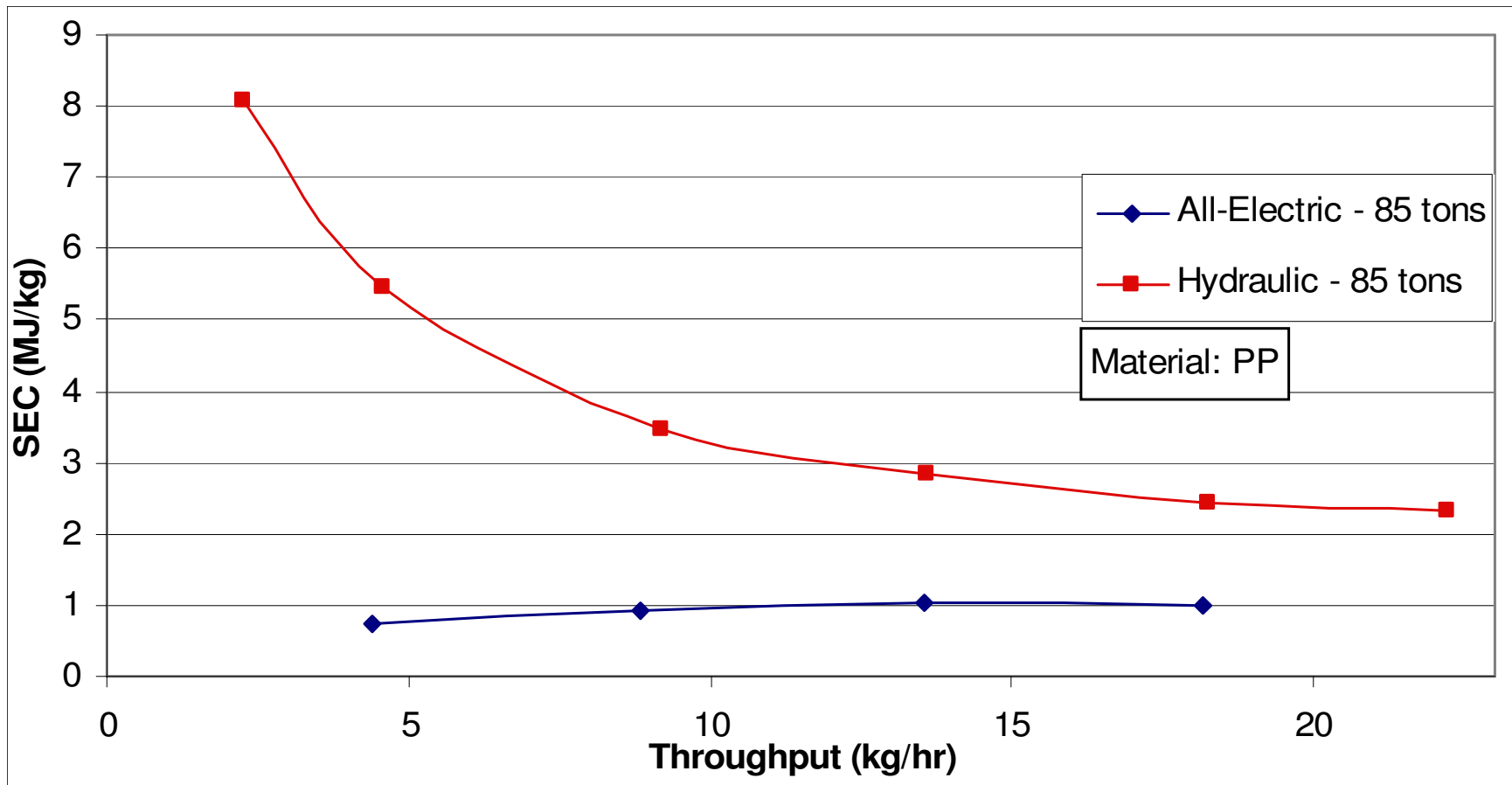


# Improve process rate

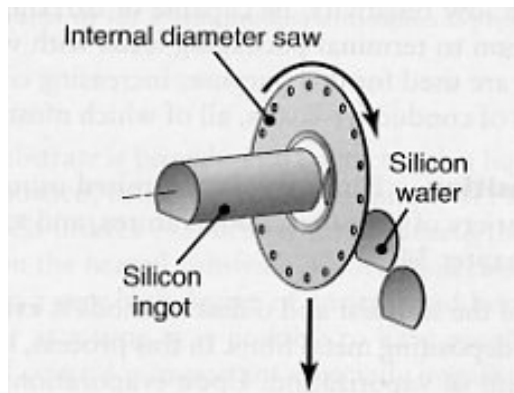


**FIGURE 22.6** Relative time required to machine with various cutting-tool materials, indicating the year the tool materials were first introduced. Note that machining time has been reduced by two orders of magnitude within a hundred years. *Source:* Courtesy of Sandvik.

# *Turn un-needed equipment off*



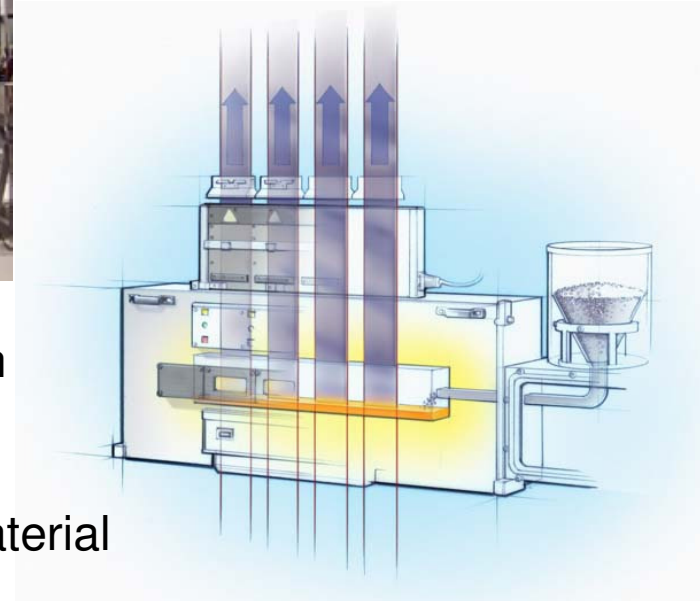
# *Use Less Materials*



In ID and wire sawing of Si ingots, the kerf material represents lost energy



String-Ribbon  
Invented by  
Ely Sachs  
saves this material



# Change Basic Mechanism

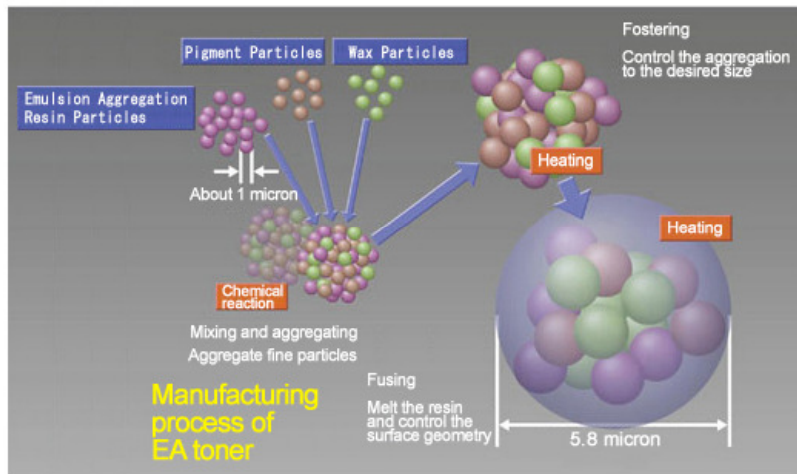


Fig. 1: Manufacturing process of EA toner

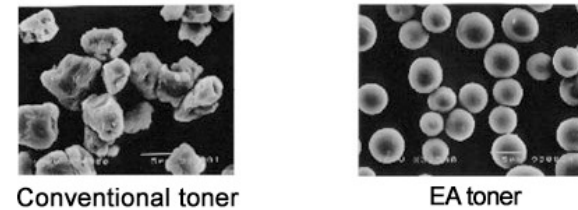
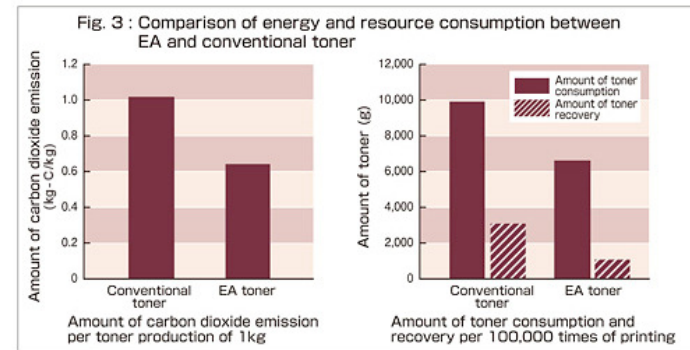


Fig. 2: Electron microscopic images of toner produced by pulverized conventional toner and EA toner

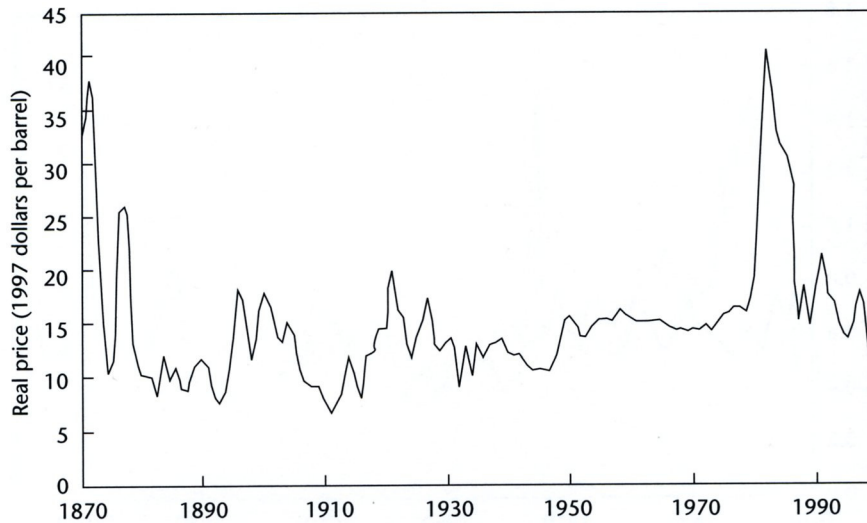


Xerox goes from grinding to emulsion polymerization  
To produce toner particles



# Increase the cost of energy!

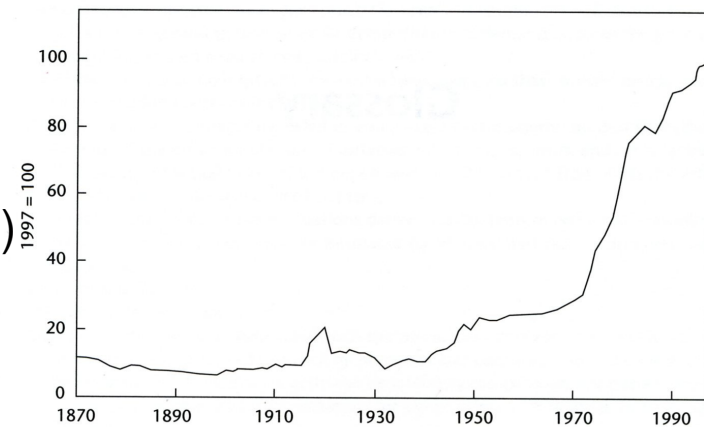
134 • Appendix: Real Prices for Selected Mineral Commodities, 1870–1997



Petroleum—U.S. Average Value, 1870–1997

SWNT cost ~ \$200/g (less for larger quantities)  
Electricity ~ 30MJ/g = 8.3 kWh  
In Massachusetts @ 0.14/kWh = \$1.17

Appendix: Real Prices for Selected Mineral Commodities, 1870–1997 • 137



All Commodities—Producer Price Index, 1870–1997

Source: