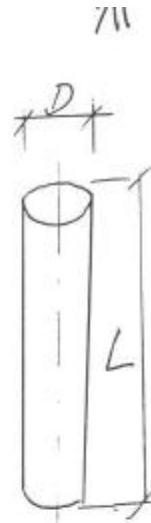


L. 810 Injection molding
HIV #6 - Solutions

Problem 1.) a) $T_{\text{mold}} = 30^\circ\text{C}$ $D = 2\text{cm}$
 $T_{\text{max}} = 100^\circ\text{C}$ $L > D$
 $T_{\text{final}} = 37^\circ\text{C}$



$$\theta = \frac{T - T_{\infty}}{T_i - T_{\infty}} = \frac{(37 - 30)^\circ\text{C}}{(100 - 30)^\circ\text{C}} = \frac{1}{10}$$

For constant temp. mold $Bi^{-1} = \frac{k}{h r_0} = 0$

$$\frac{r}{r_0} = 0 \text{ @ centerline}$$

From Fig. 5.8 in "Transient Conduction" handout: $F_0 \approx 0.5$ for a cylinder

$$F_0 = \frac{\alpha t}{r_0^2}$$

$$0.5 = \frac{(10^{-3} \text{ cm}^2/\text{s}) t}{(1 \text{ cm})^2}$$

$$\Rightarrow t = 500 \text{ s}$$

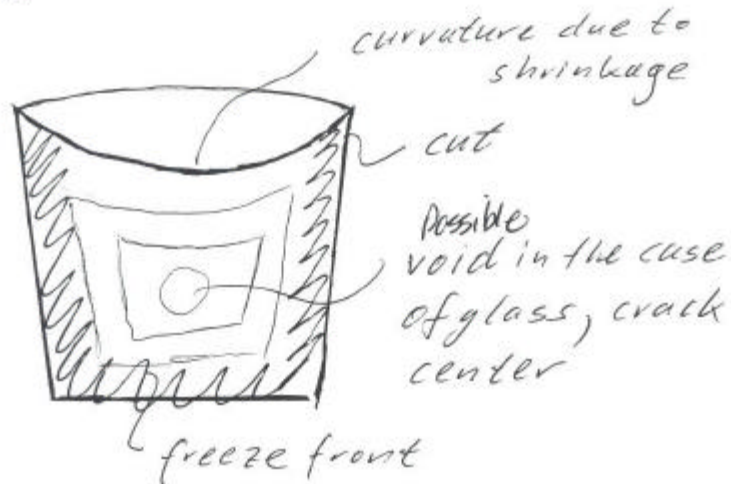
If L and D were of the same order then the heat loss to the mold thru the bottom surface would become significant relative to the heat loss thru the sides. Cooling time would be reduced. (cont)

2.810 Injection Molding
HW # 6 - Solutions

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Problem #1) (cont)

b) Solidified candle w/ $L = D$



Wax next to walls solidifies first. Wax in center cools and shrinks causing a depression. Finally case of "hydrostatic tension" may occur in very center which is last to solidify and is constrained by neighboring already solidified material.

2.810 Injection Molding 3/11

HW # 6 - Solutions

Problem 2.)

1) Cooling Time

Max. wall thickness: $D = 0.16 \text{ cm}$

$$\Rightarrow D/2 = L = 0.08 \text{ cm}$$

from handout $t_{\text{cool}} \approx \frac{L^2}{\alpha}$

with $\alpha \approx 10^{-3} \text{ cm}^2/\text{s}$ diffusivity for polymers

$$\Rightarrow \underline{t_{\text{cool}} = 6.4 \text{ s}}$$

2) Special Features

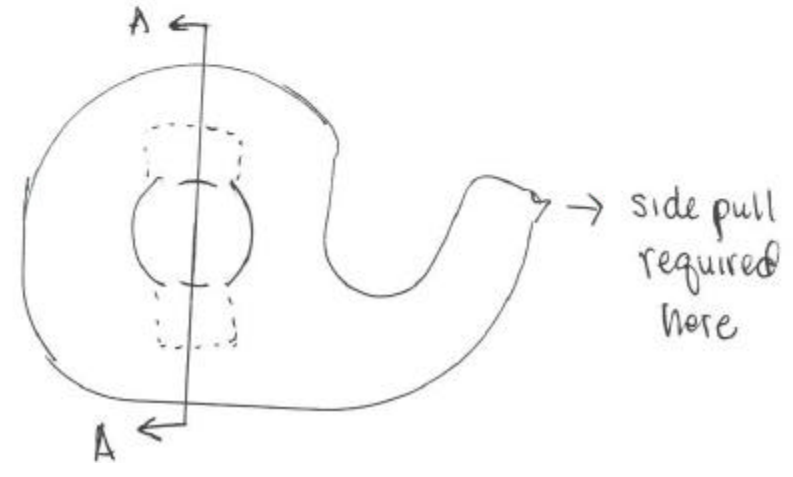
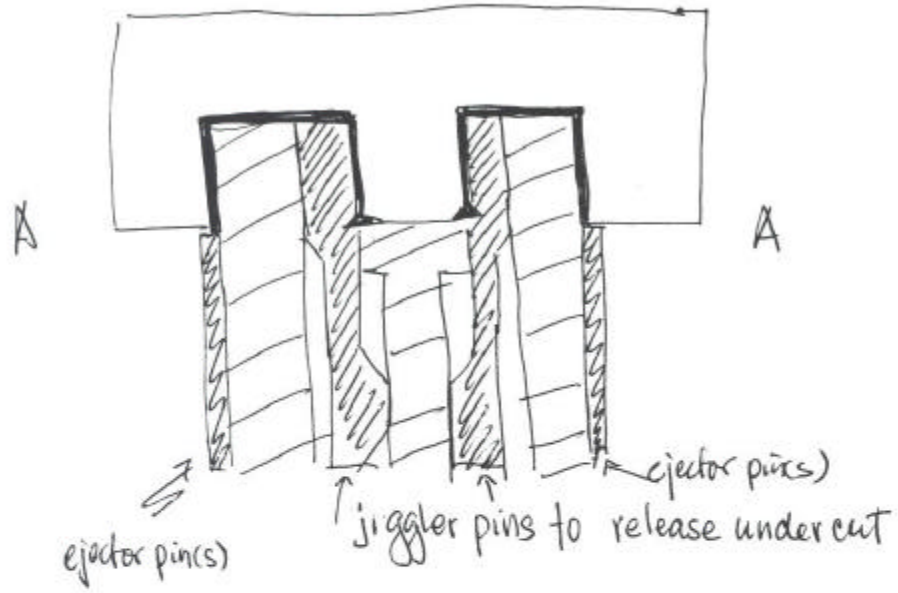
- 2 undercuts require special tool features
- serrated edge requires side pull
- ejector pins to remove part (see attached drawing)

3) Mold Filling Sequence



(cont')

Some features of the tooling for the plastic tape dispenser 4



2.810 - Injection Molding 5/11
HW #6 - Solutions

Problem 2) cont 1

4) Machine Requirements

Clamp Force: $F = p \cdot A_{proj} \cdot n_{cavity}$

injection pressure: $p \approx 10,000 \text{ psi}$

projected area: $A \approx 2.5 \times 2.5 \text{ in}^2 = 6.25 \text{ in}^2$

number of cavities: $n_{cav} = 4$ (assume here)

$$\Rightarrow F = 250,000 \text{ lb} \hat{=} 125 \text{ tons}$$

(Note: conservative estimate, large area includes runner, 10ksi probably on high side
see Boothroyd, Dewhurst & Knight p332 in handout)

Shot Size

$$\text{wt/part} = 0.5 \text{ oz} \Rightarrow 4 \text{ cavities} \Rightarrow 2.0 \text{ oz wt}$$

$$2.0 \text{ oz wt} \cdot 28 \text{ oz/g} = 56 \text{ g}$$

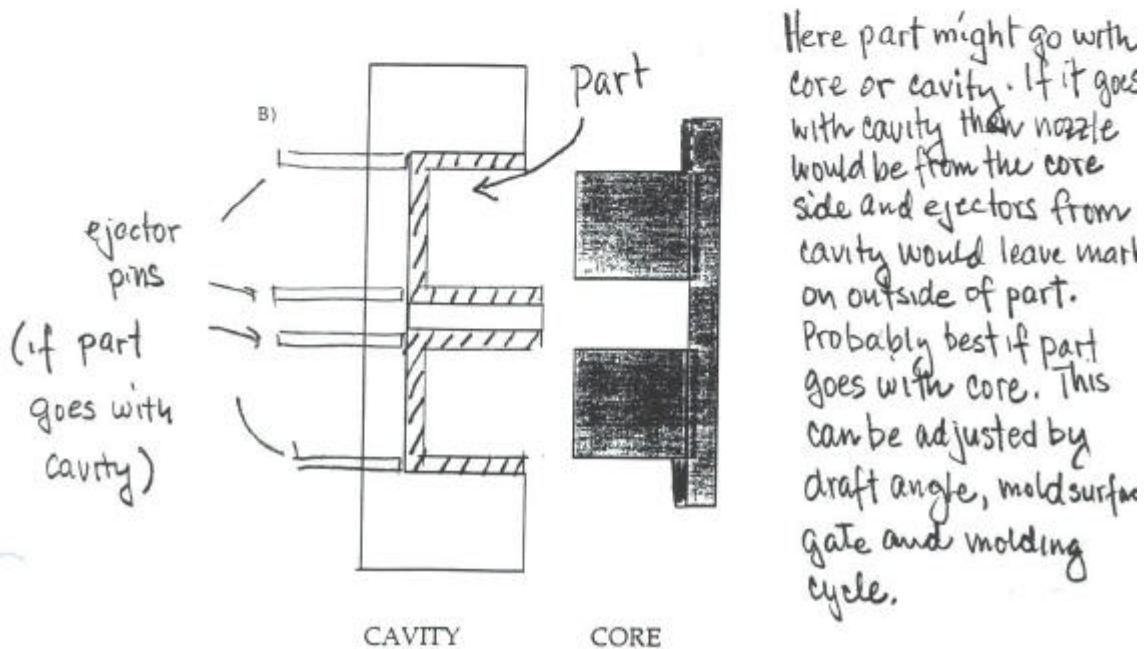
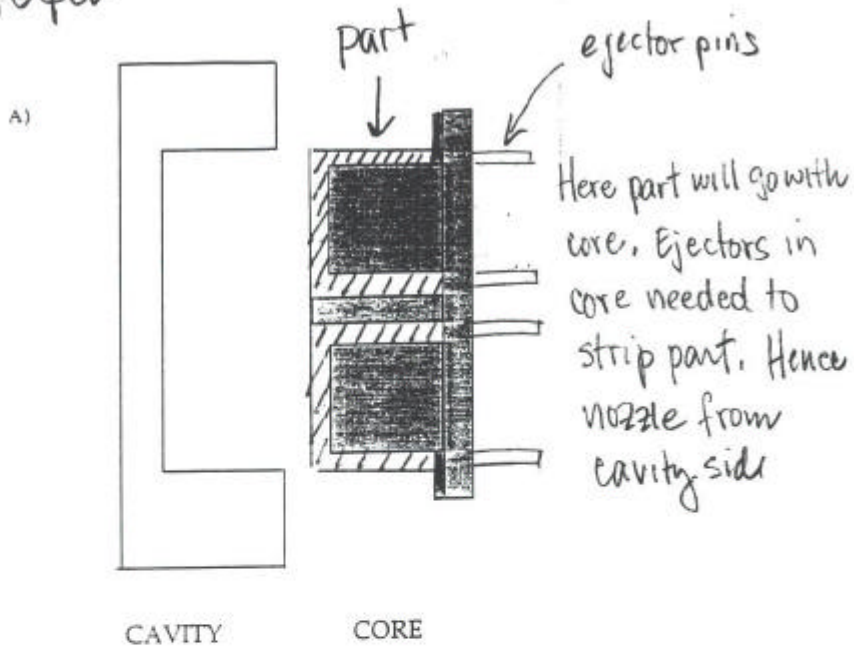
$$56 \text{ g} / 1.3 \text{ g/cm}^3 = \underline{43.1 \text{ cm}^3} \hat{=} \underline{1.43 \text{ oz. fl}}$$

A shot size of at least 1.43 oz. fl. is required to injection mold 4 parts at once. Note: LMP Machine: 1.5 oz.

Note that runner system may add something like 37% for a 16 cm^3 part - our parts are 14 cm^3 each. See Table 8.2 in Boothroyd, Dewhurst & Knight handouts.

Injection Molding Homework Sol'n
 #3 a, c & d

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Injection Molding Homework Solution HW#6

Problem #3/b)

Design Alterations/DFM

- Add draft angle
- Round corners
- Make walls same thickness
- Eliminate "overhang" if possible



Estimate Part Cycle Time:

$$t \approx \frac{H^2}{\alpha} = \frac{(0.635 \text{ cm}/2)^2}{(10^{-3} \text{ cm}^2/\text{sec})} = 101 \text{ sec.}$$

(This time is too long, so redesign with thinner walls and ribs if necessary to stiffen.)

Clamping Force (not asked for, but here it is)

$$\begin{aligned} \text{Projected area} &\approx (4.50 + 0.50) \times (3.50 + 0.50) \\ &\approx 20 \text{ in}^2 + \text{runner} \end{aligned}$$

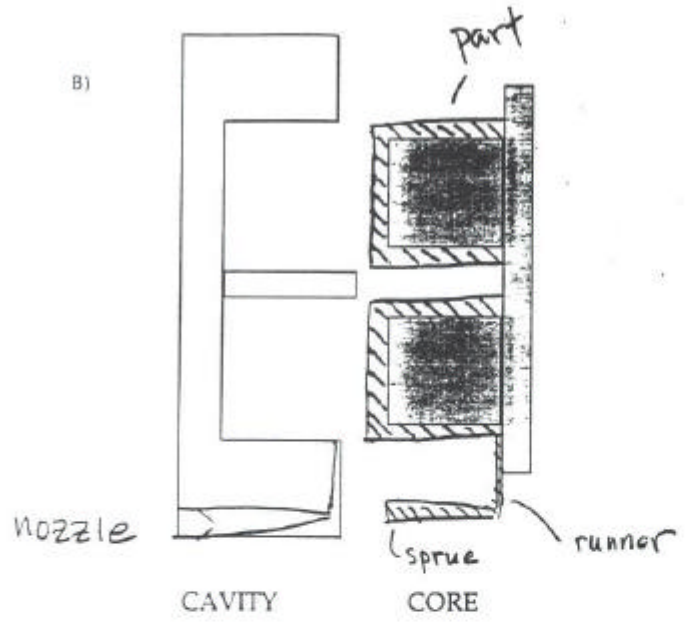
$$\text{Pressure} \approx 7000 \text{ psi}$$

eliminate in redesign

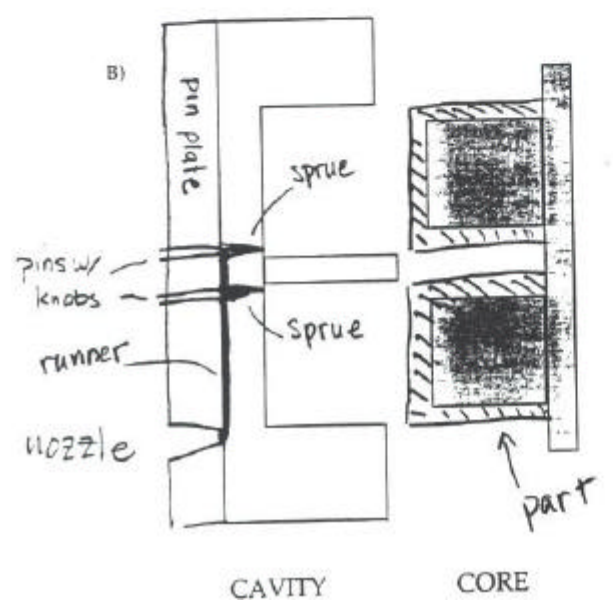
$$\begin{aligned} \text{Clamp force} &\approx 20 \text{ in}^2 \times 7000 \frac{\text{lb}}{\text{in}^2} = 140,000 \text{ lbs} \\ &= 70 \text{ tons} \end{aligned}$$

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3e)



3f



9/11

#4 Consider transport rate / cooling rate (units $\frac{1}{\text{time}}$)

for injection molding

$$\text{transport } \frac{1}{t} \sim \frac{V}{L_x} \rightarrow \frac{1}{4} \frac{\sqrt{L_z}}{\alpha} \cdot \frac{L_z}{L_x}$$

$$\text{cooling } \frac{1}{t} \sim \frac{\alpha}{(L_z/2)^2}$$

$$\text{typical values are } \frac{1}{4} \frac{10 \frac{\text{cm}}{\text{s}} \times 0.1 \text{cm}}{10^{-3} \frac{\text{cm}^2}{\text{s}}} \times \frac{0.1 \text{cm}}{10 \text{cm}}$$

$$\approx 2.5$$

hence the two rates are about equal within one order of magnitude.

10/11

for die casting typical values are

$$\frac{1}{4} \frac{10 \frac{\text{cm}}{\text{s}} \times 0.1 \text{cm}}{.3 \frac{\text{cm}^2}{\text{s}}} \times \frac{0.1}{10} = 10^{-2}$$

Hence the heat transfer rate is much faster and there is the danger of a thin runner system from solidifying before the molds are filled. (Note that the actual situation is a little better than this because the heat transfer rate is smaller due to film resistance)

Note that the multicavity tool for die casting shown in Fig 4 does not show overflow well commonly use. See p.413 handout Design for Die Cast

5) eqn 8.5 in Beethroyd et al is

$$t_c = \frac{h_{\max}^2}{\pi^2 \alpha} \ln \frac{4(T_i - T_m)}{\pi(T_x - T_m)}$$

$$\text{let } \frac{T_x - T_m}{T_i - T_m} = 0.1$$

$$\begin{aligned} t_c &= \frac{h_{\max}^2}{4\alpha} \times \frac{4}{\pi^2} \ln \frac{40}{\pi} \\ &= 1.03 \times \frac{(h_{\max}/2)^2}{\alpha} \end{aligned}$$